



SIGNAL  
ANALYSIS &  
IMAGING GROUP

# **3D deblending and reconstruction with interpolated MSSA for arbitrary irregular-grid compressive simultaneous-source data**

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## 1. Introduction

## 2. Method

- Conventional MSSA method with binning strategy
- Interpolated-MSSA (I-MSSA) method

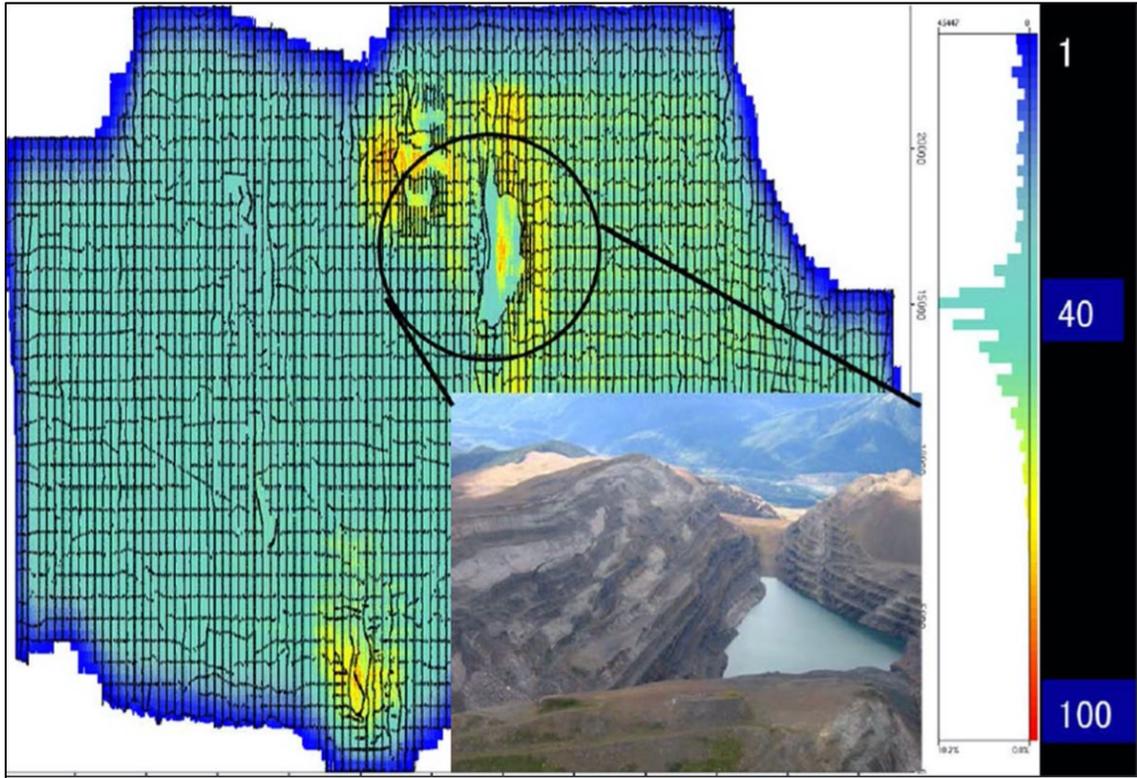
## 3. Synthetic example

- Without random noise
- With random noise

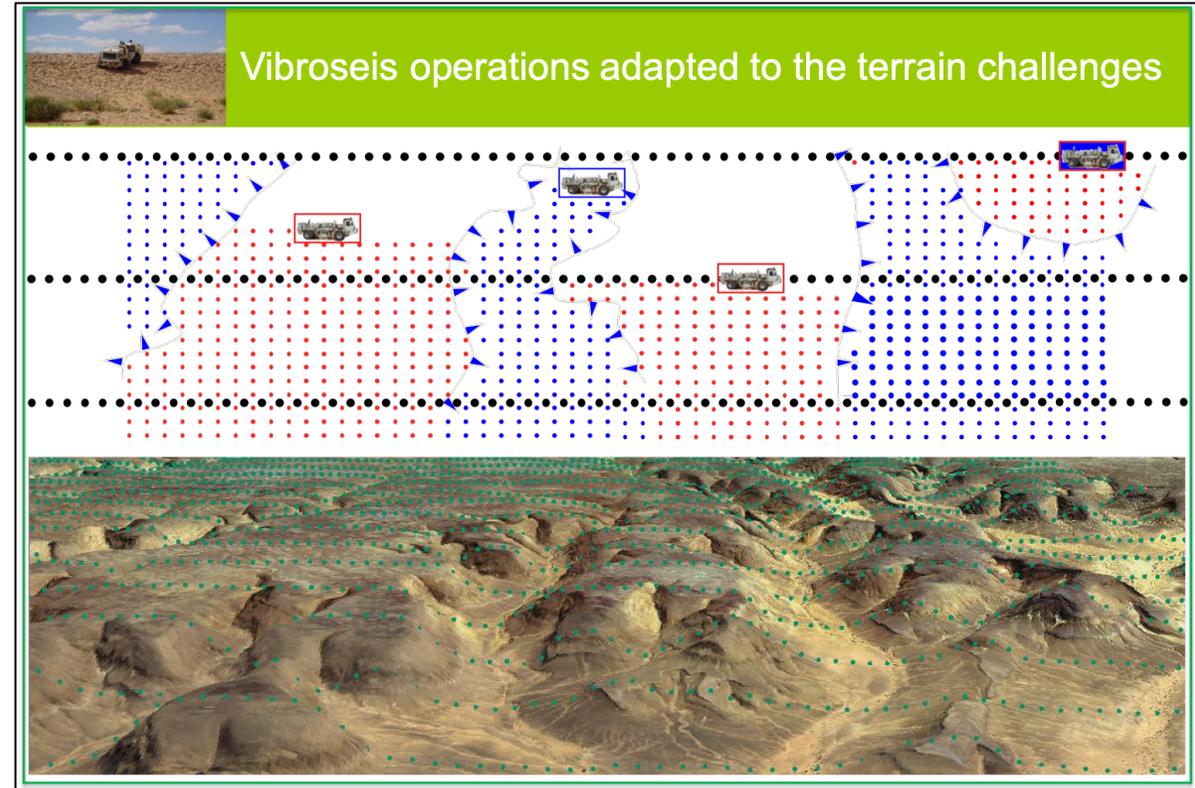
## 4. Real data example

## 5. Conclusion

## 6. Acknowledgement



(Trad,2008)



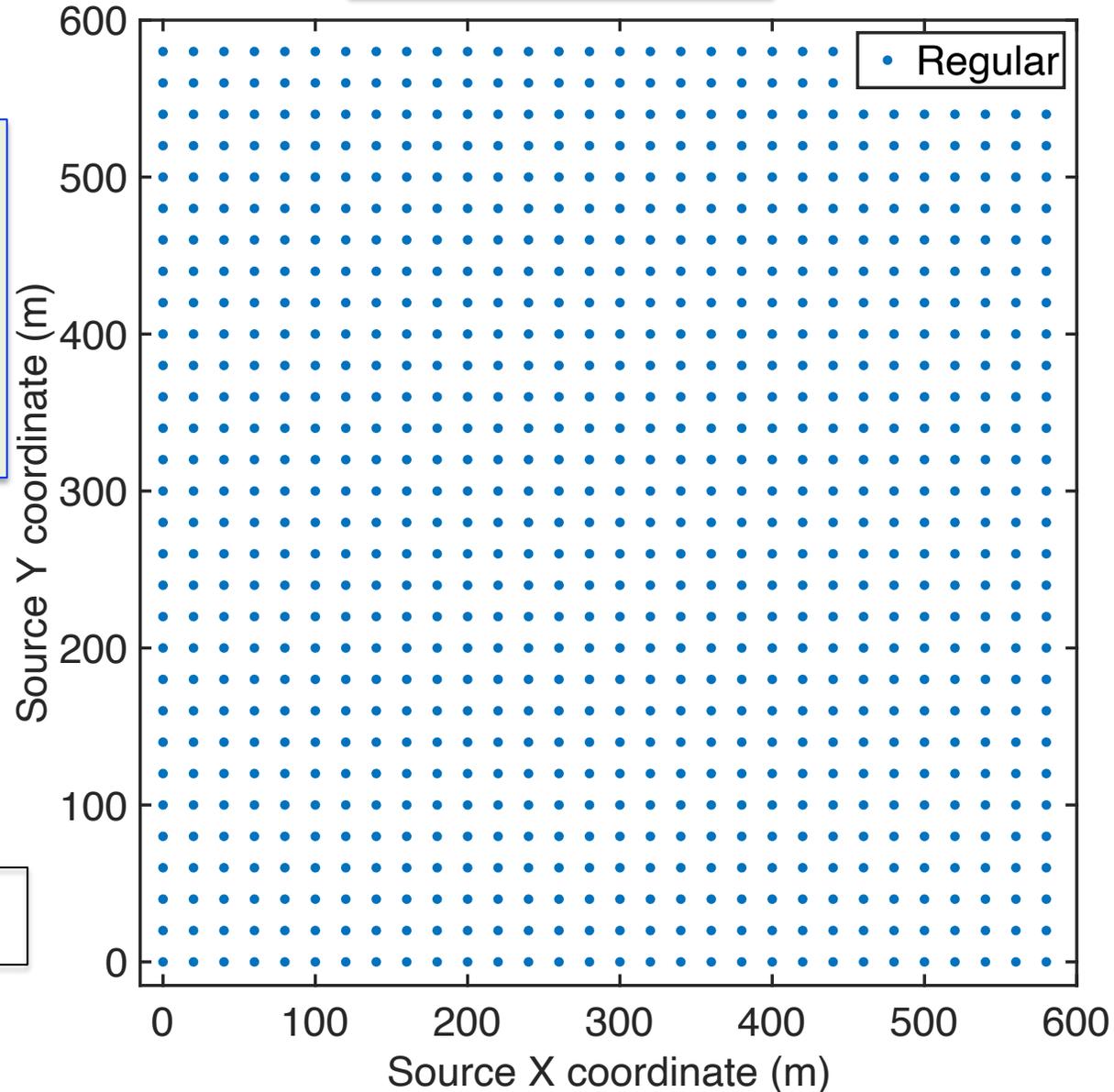
(Ray Abma, 2010)

- Toy example

**3D seismic acquisition  
= 5D seismic data  
(t,sx,sy,rx,ry)**

**1 CRG is a 3D cube**

**Source location**

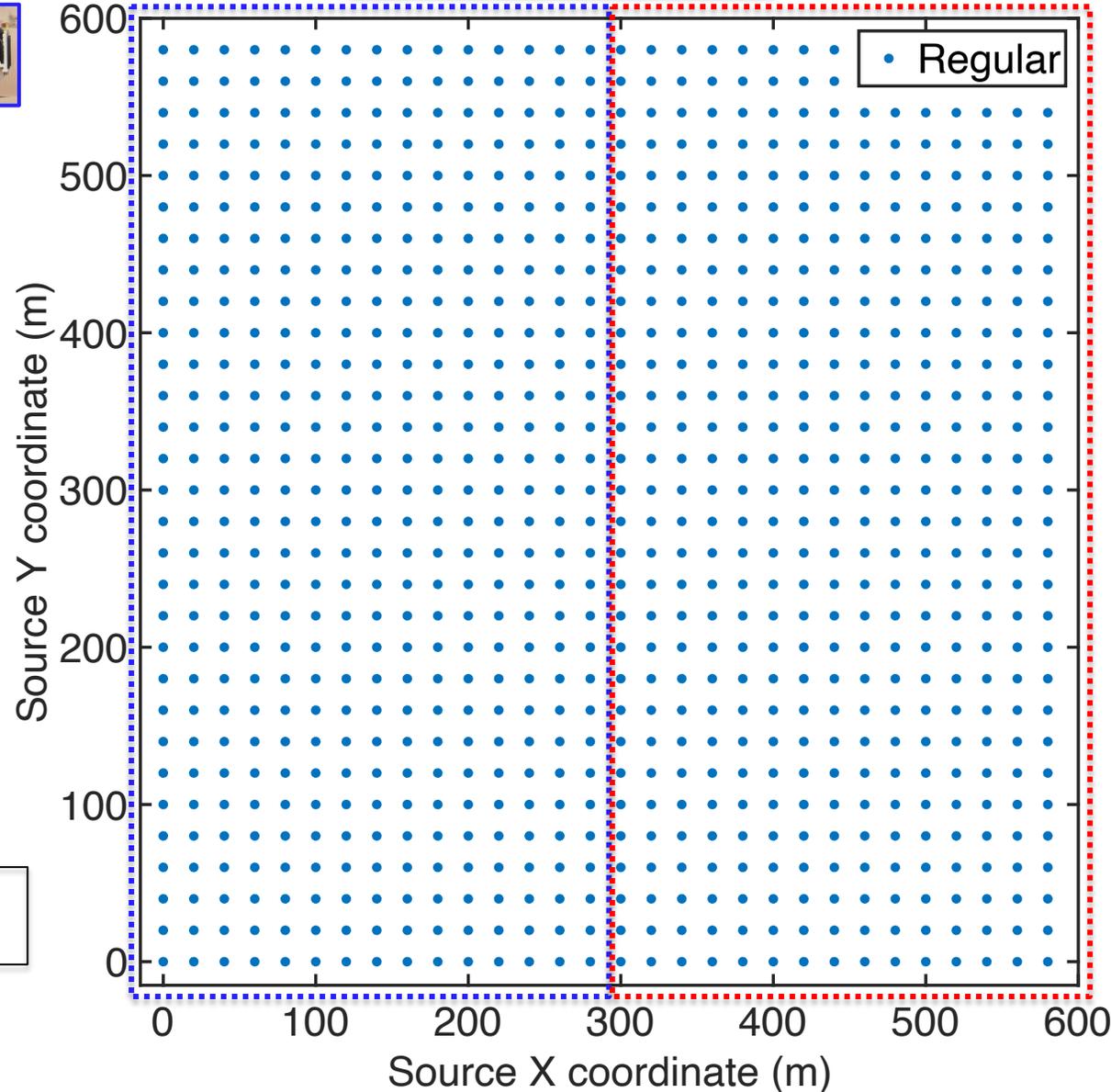


• Regular source location

Source 1



Source location



Source 2



**3D Simultaneous-  
source acquisition  
(BF=2)**

**= 5D seismic data  
( $t, s_x, s_y, r_x, r_y$ )**

**1 CRG is a 3D cube**

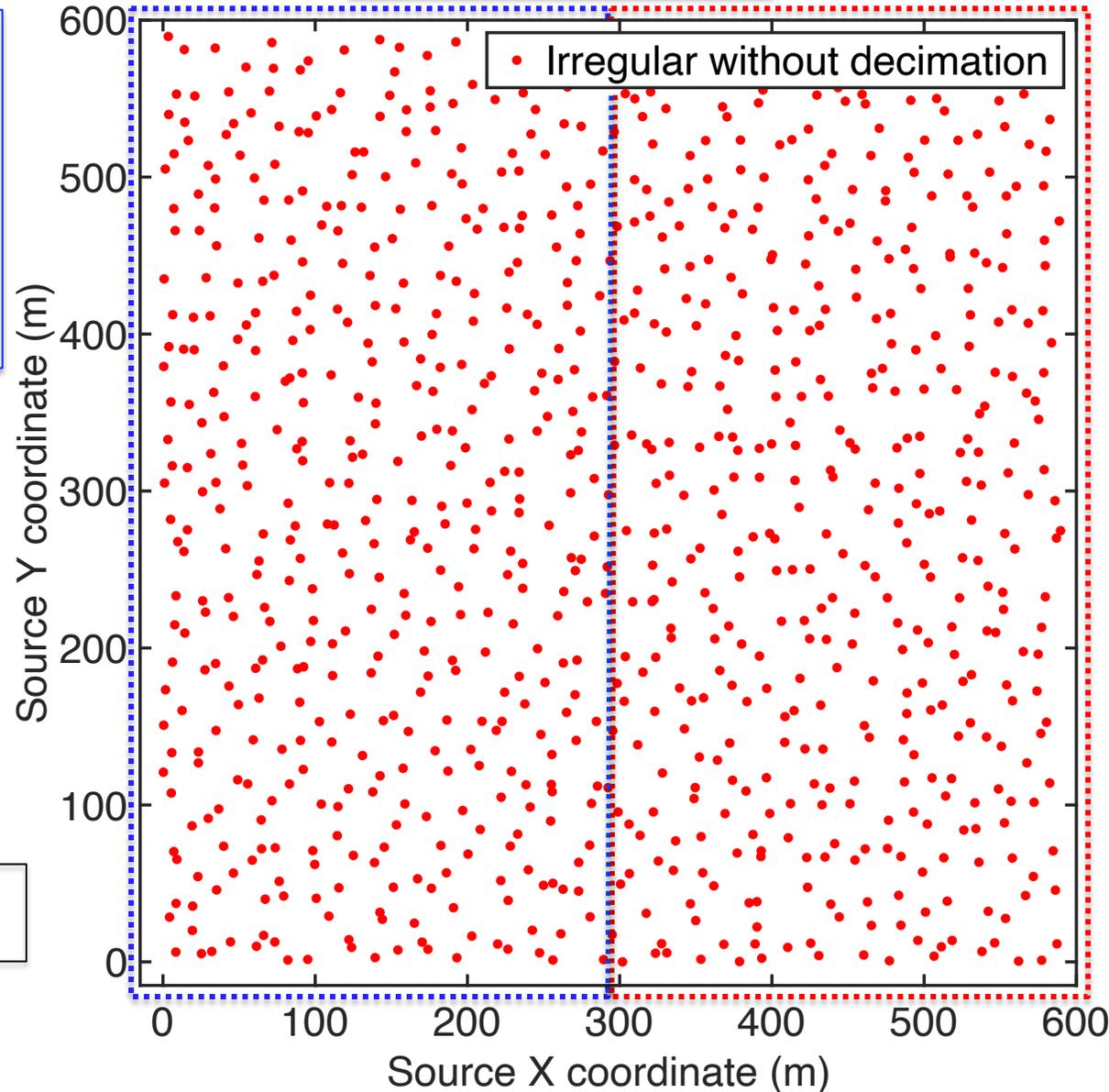
• Regular source location

- *Conventional acquisition: 10 days*
- *Blending acquisition (BF=2):  
≈ 5 days*

3D seismic acquisition  
= 5D seismic data  
( $t, s_x, s_y, r_x, r_y$ )

1 CRG is a 3D cube

Source location



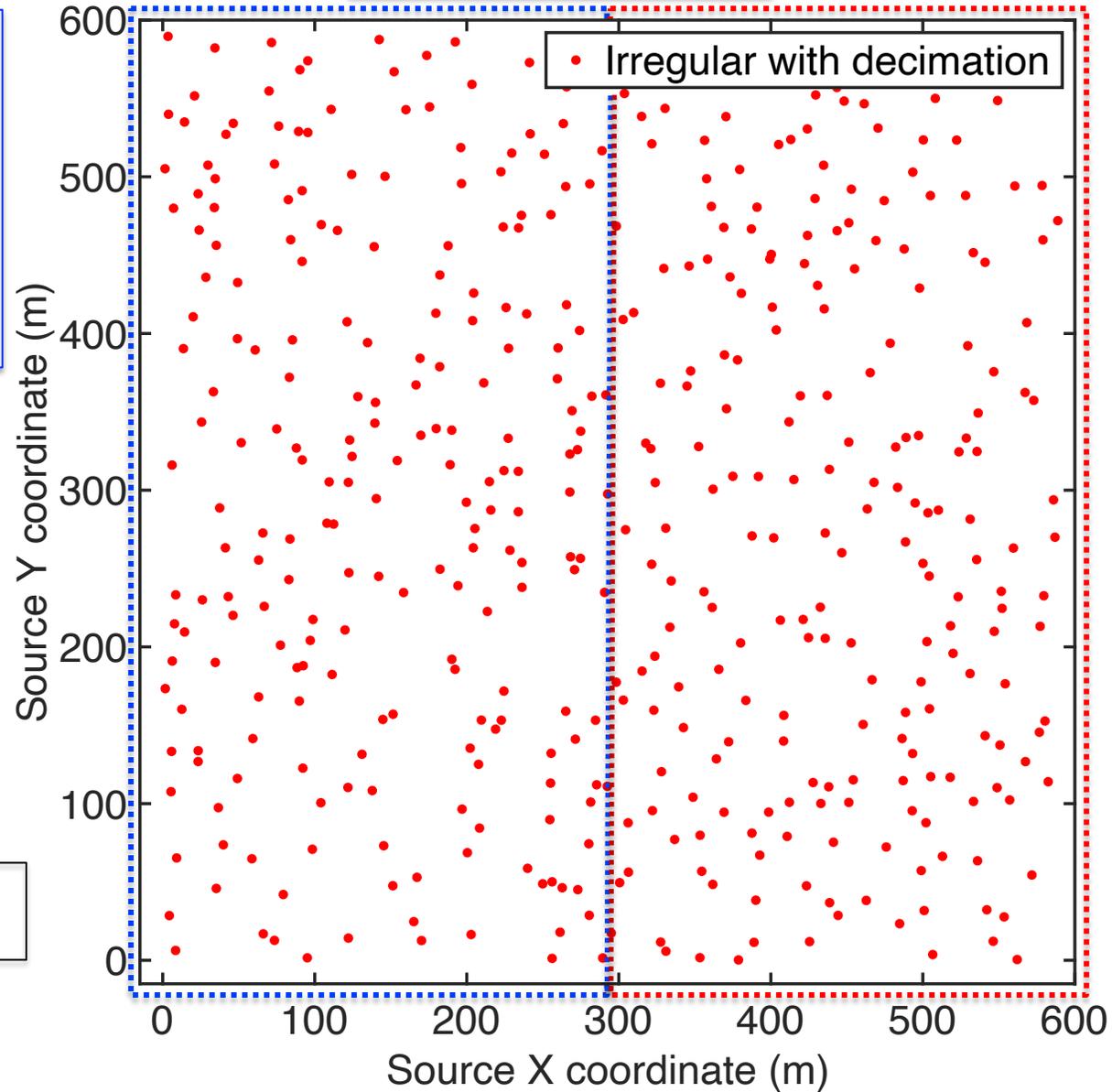
• Irregular source location

- *Conventional acquisition: 10 days*
- *Blending acquisition (BF=2): ≈ 5 days*

3D seismic acquisition  
= 5D seismic data  
( $t, s_x, s_y, r_x, r_y$ )

1 CRG is a 3D cube

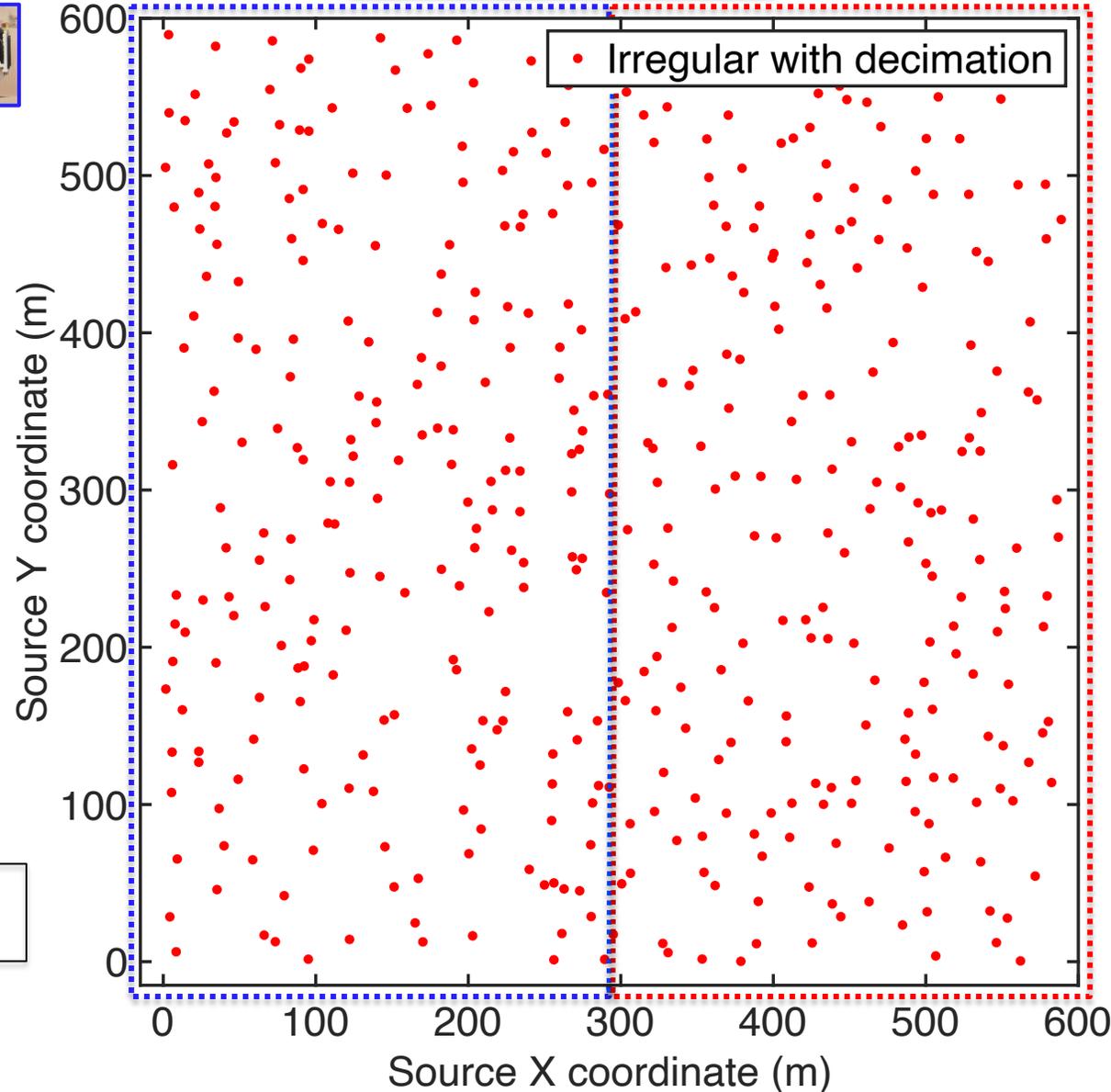
Source location



Source 1



Source location



Source 2



**3D Simultaneous-source acquisition (BF=2)**

**+ 50% shot number decimation**

**= 5D seismic data (t,sx,sy,rx,ry)**

**1 CRG is a 3D cube**

*Dec* = 50% decimation

$$T_{obs} = \frac{T_{conv}}{BF} * (1 - Dec)$$

- *Conventional acquisition: 10 days*
- *Blending acquisition (BF=2): ≈ 5 days (Time compression)*
- *Compressive blending acquisition (dec=50%): ≈ 2.5 days (Spatial compression)*

Source 1



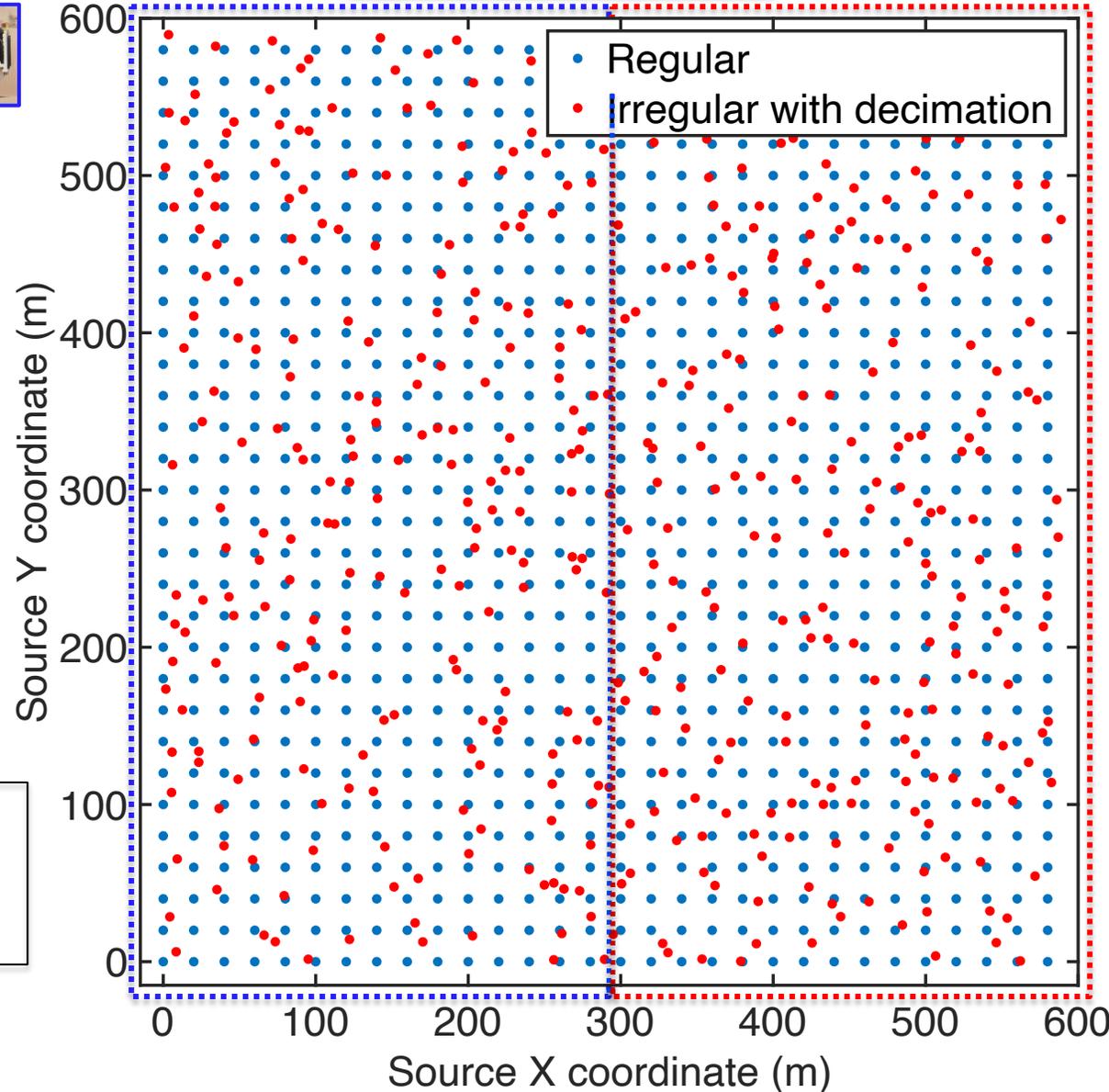
**3D Simultaneous-source acquisition (BF=2)**

**+ 50% shot number decimation**

**= 5D seismic data (t,sx,sy,rx,ry)**

- Regular source location
- Irregular source location

Source location



Source 2



**1 CRG is a 3D cube**

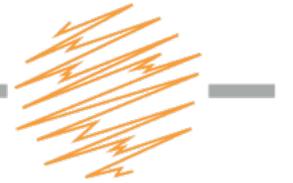
*Dec* = 50% decimation

$$T_{obs} = \frac{T_{conv}}{BF} * (1 - Dec)$$

- *Conventional acquisition: 10 days*
- *Blending acquisition (BF=2): ≈ 5 days (Time compression)*
- *Compressive blending acquisition (dec=50%): ≈ 2.5 days (Spatial compression)*

# Deblending + Irregular Reconstruction

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- MSSA with binning

$$J = \|\mathbf{b} - \mathcal{B}\mathcal{T}\mathbf{D}\|_2^2 \quad s.t. \quad rank(\mathbf{D}) \leq k$$



$$\mathcal{T}_{ij} = \begin{cases} 1 & \text{if one trace is assigned to grid point } (i, j) \\ 0 & \text{if grid point } (i, j) \text{ is empty} \end{cases}$$

- I-MSSA

$$J = \|\mathbf{b} - \mathcal{B}\mathcal{W}\mathbf{D}\|_2^2 \quad s.t. \quad rank(\mathbf{D}) \leq k$$

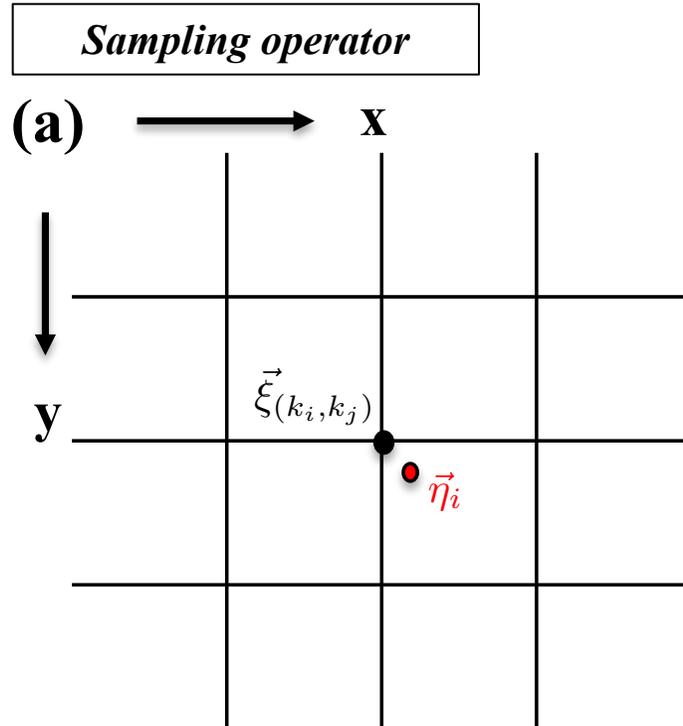


$\mathcal{W}$  : regular  $\rightarrow$  irregular

$\mathcal{W}^*$  : irregular  $\rightarrow$  regular

- Sinc-Kaiser interpolator**  $\mathcal{W}_k(t) = \text{sinc}(\pi t) \frac{I_0\left(a\sqrt{1 - (t/(N+1))^2}\right)}{I_0(a)}$

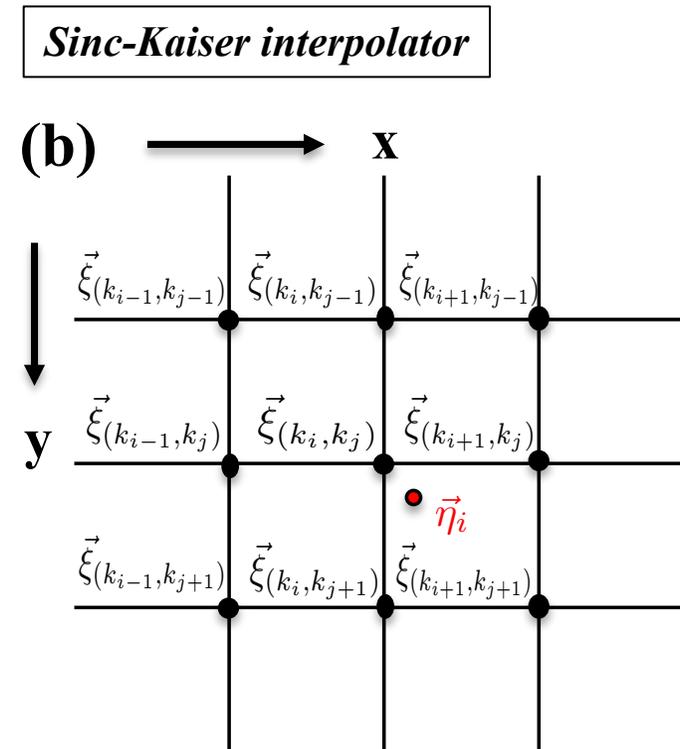
- MSSA with binning



$$\mathbf{D}^\nu = \mathcal{P}[\mathbf{D}^{\nu-1} - \lambda \mathcal{F}^* \mathcal{B}^* (\mathcal{B} \mathcal{F} \mathbf{D}^{\nu-1} - \mathbf{b})]$$

**Projection operator = Multichannel Singular Spectrum Analysis (MSSA)**

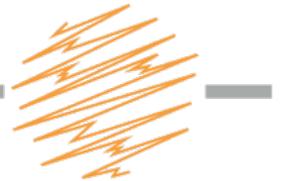
- I-MSSA

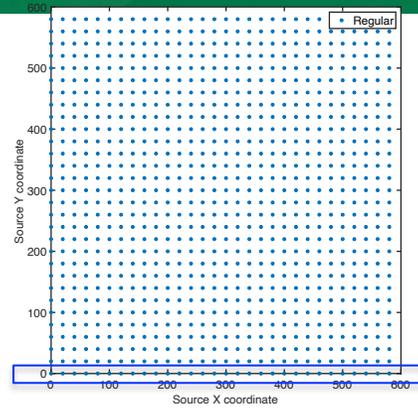


$$\mathbf{D}^\nu = \mathcal{P}[\mathbf{D}^{\nu-1} - \lambda \mathcal{W}^* \mathcal{B}^* (\mathcal{B} \mathcal{W} \mathbf{D}^{\nu-1} - \mathbf{b})]$$

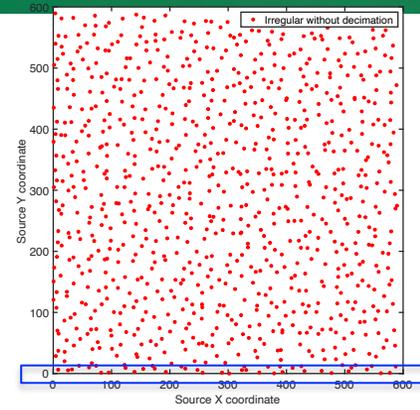
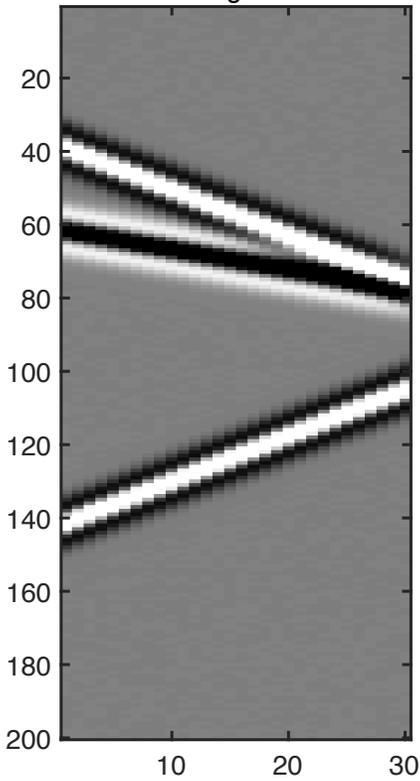
Blending noise (BF=2) + 50% decimation

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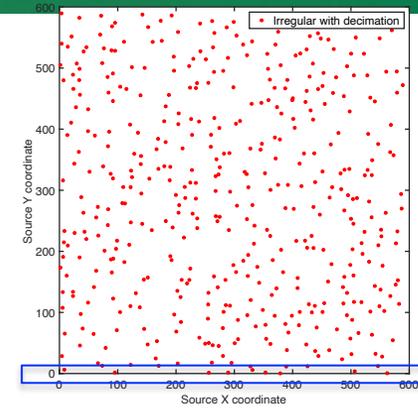
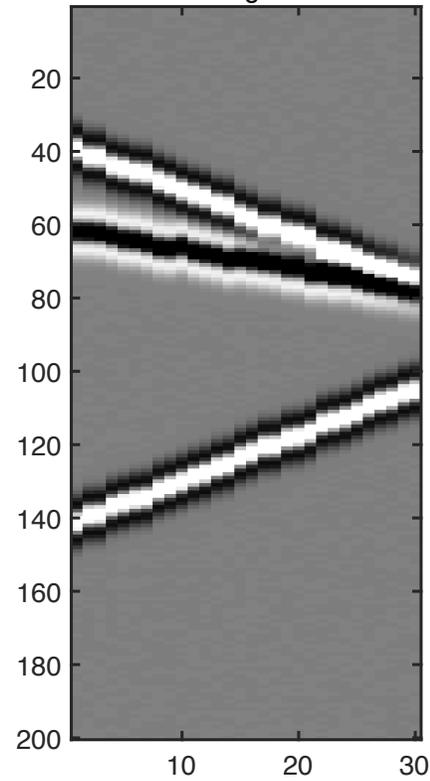




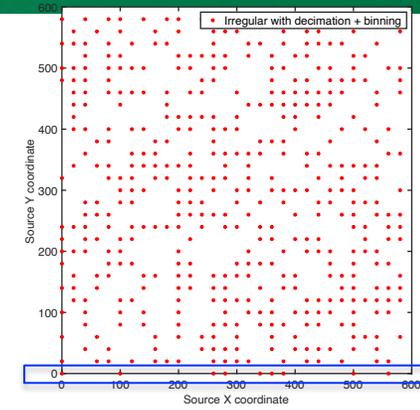
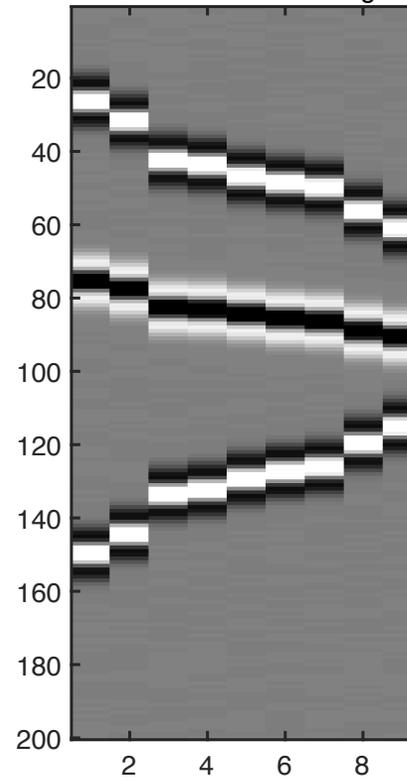
Clean regular data



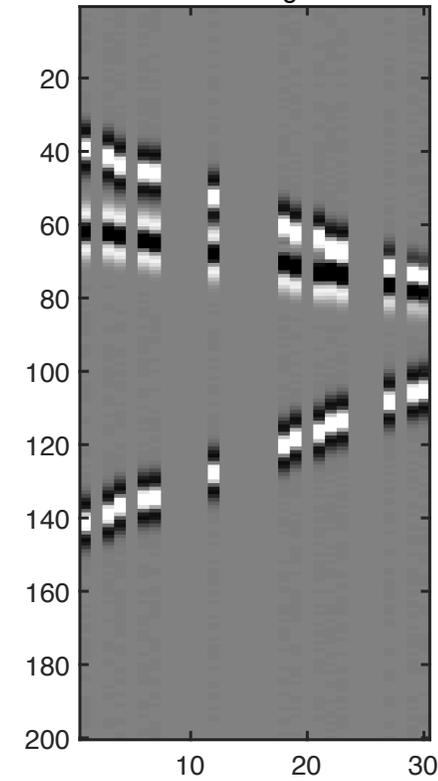
Clean irregular data



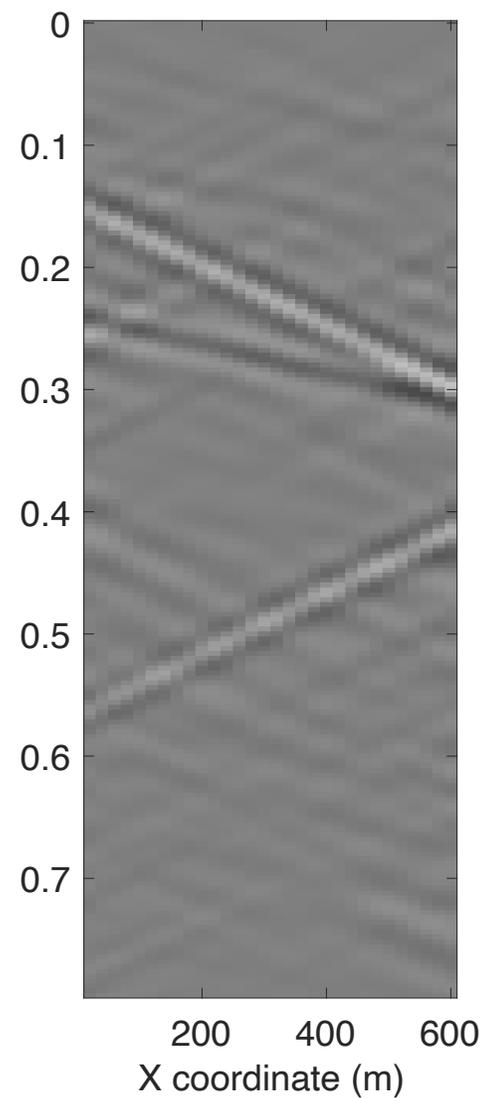
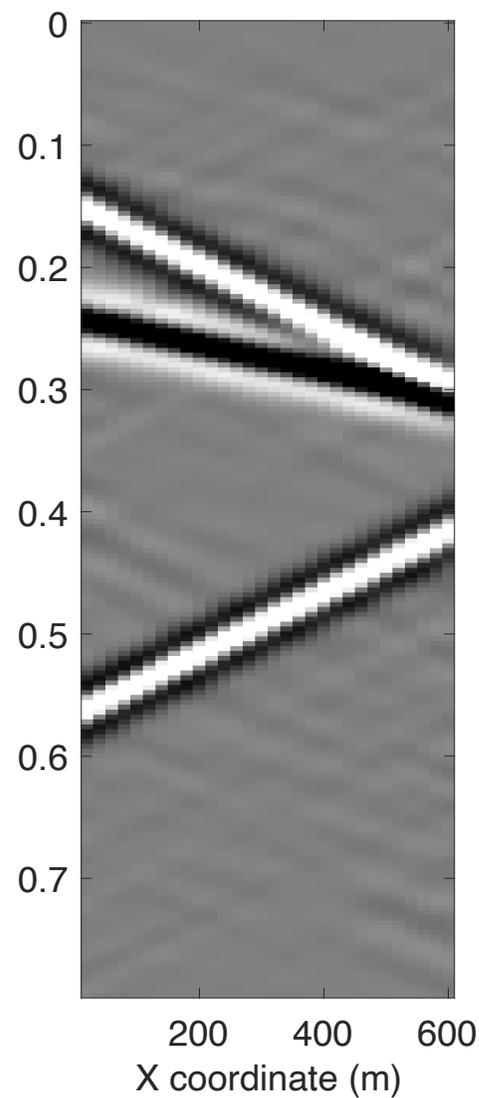
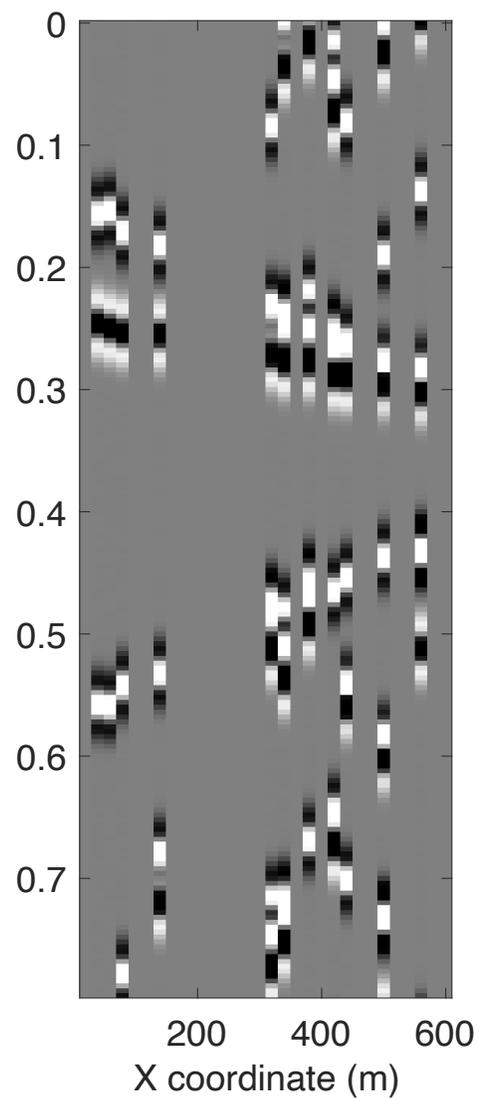
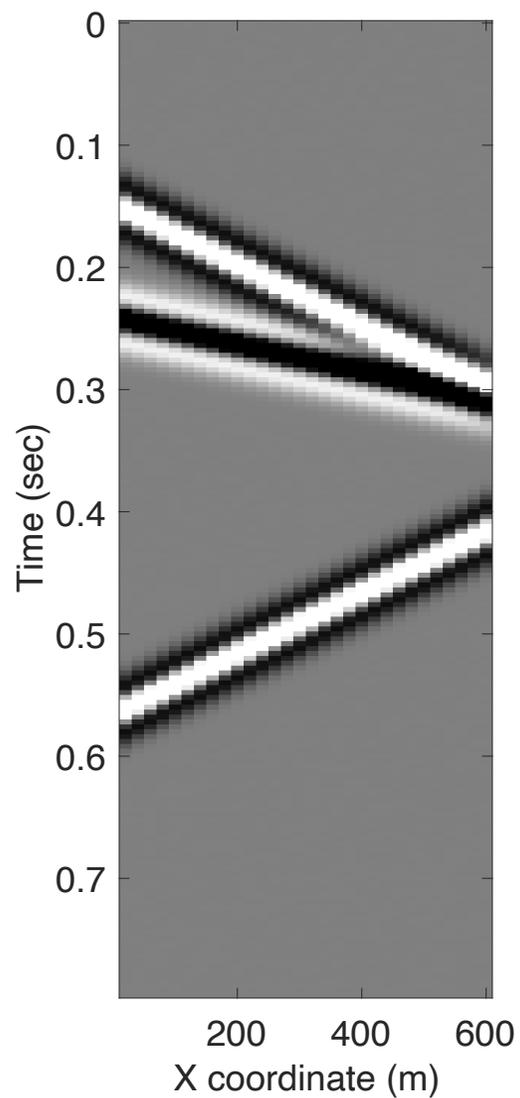
Observed real clean irregular



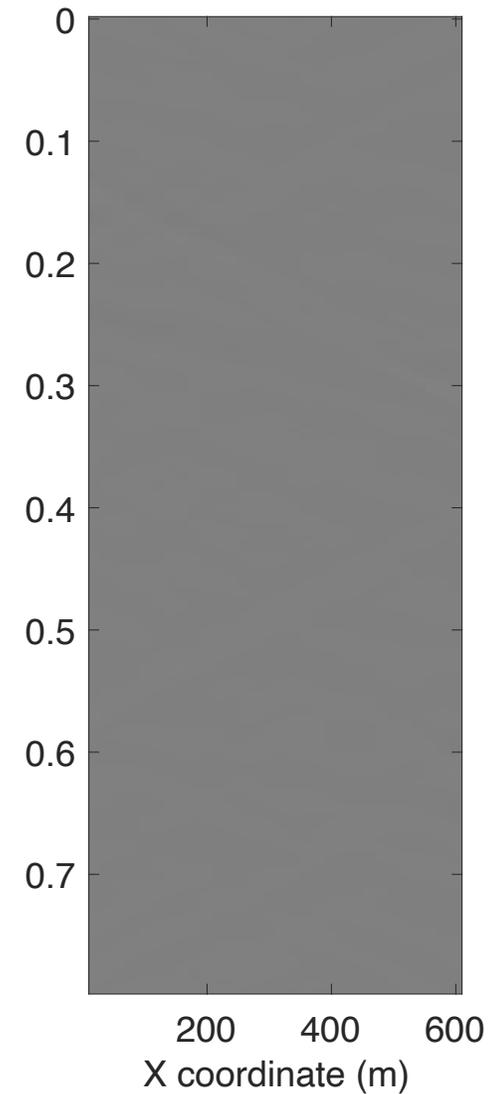
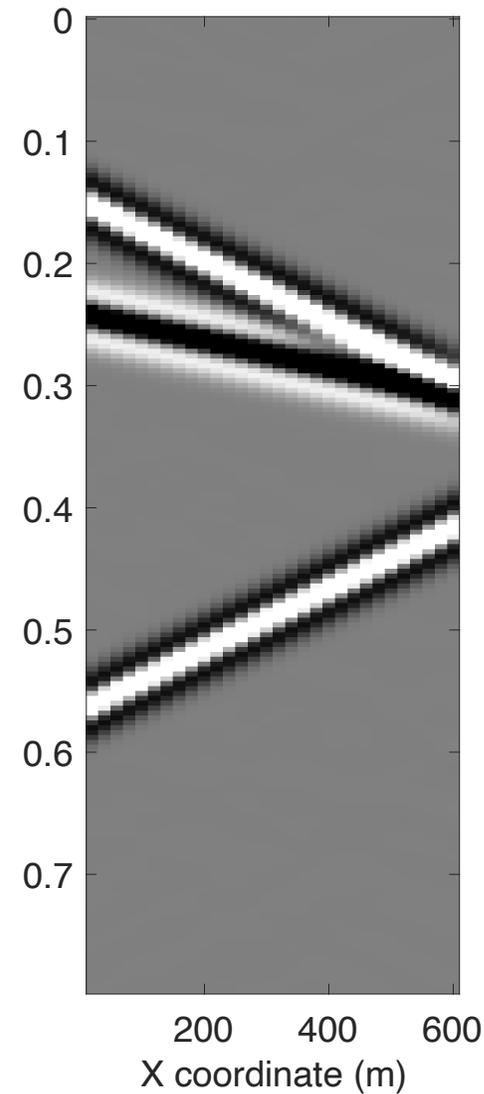
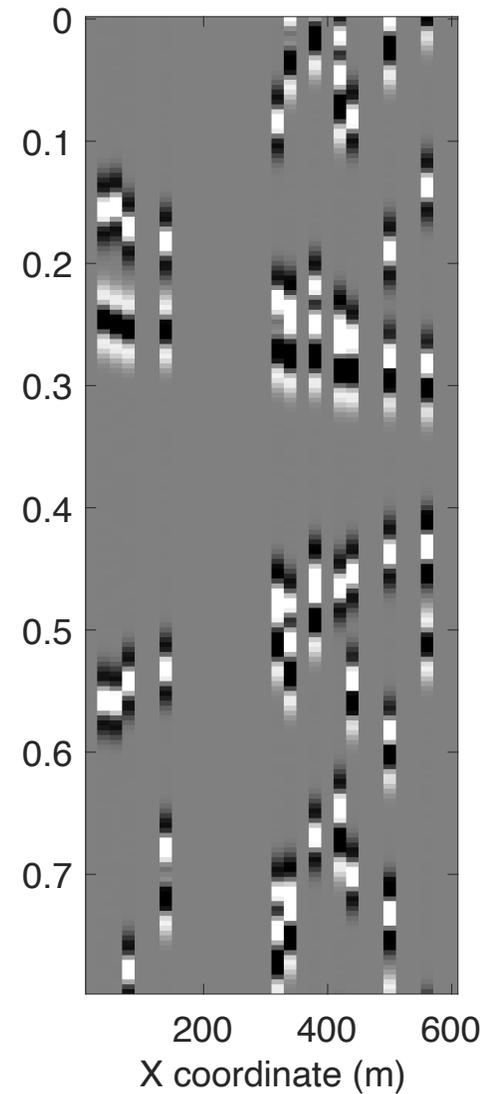
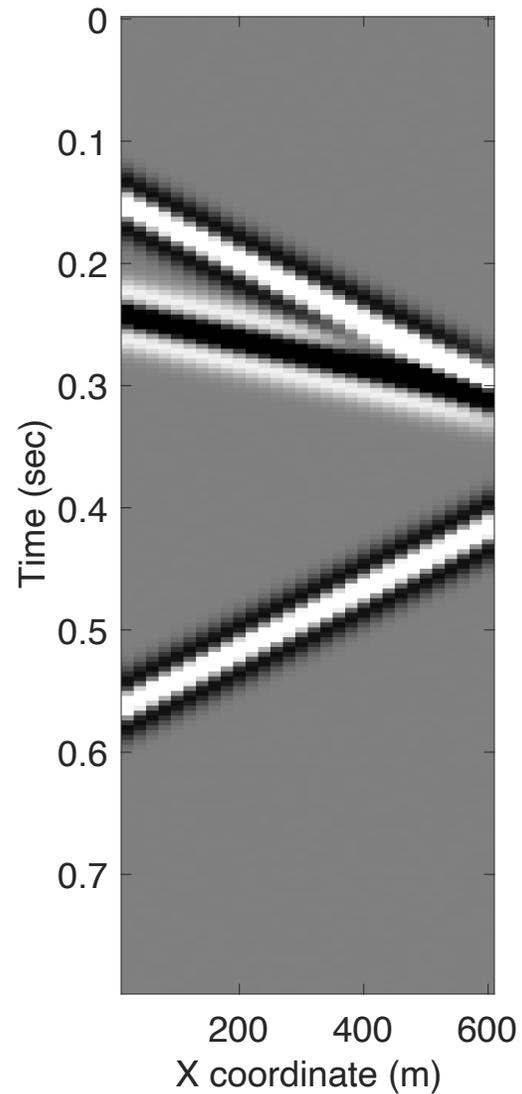
Observed clean irregular + binning

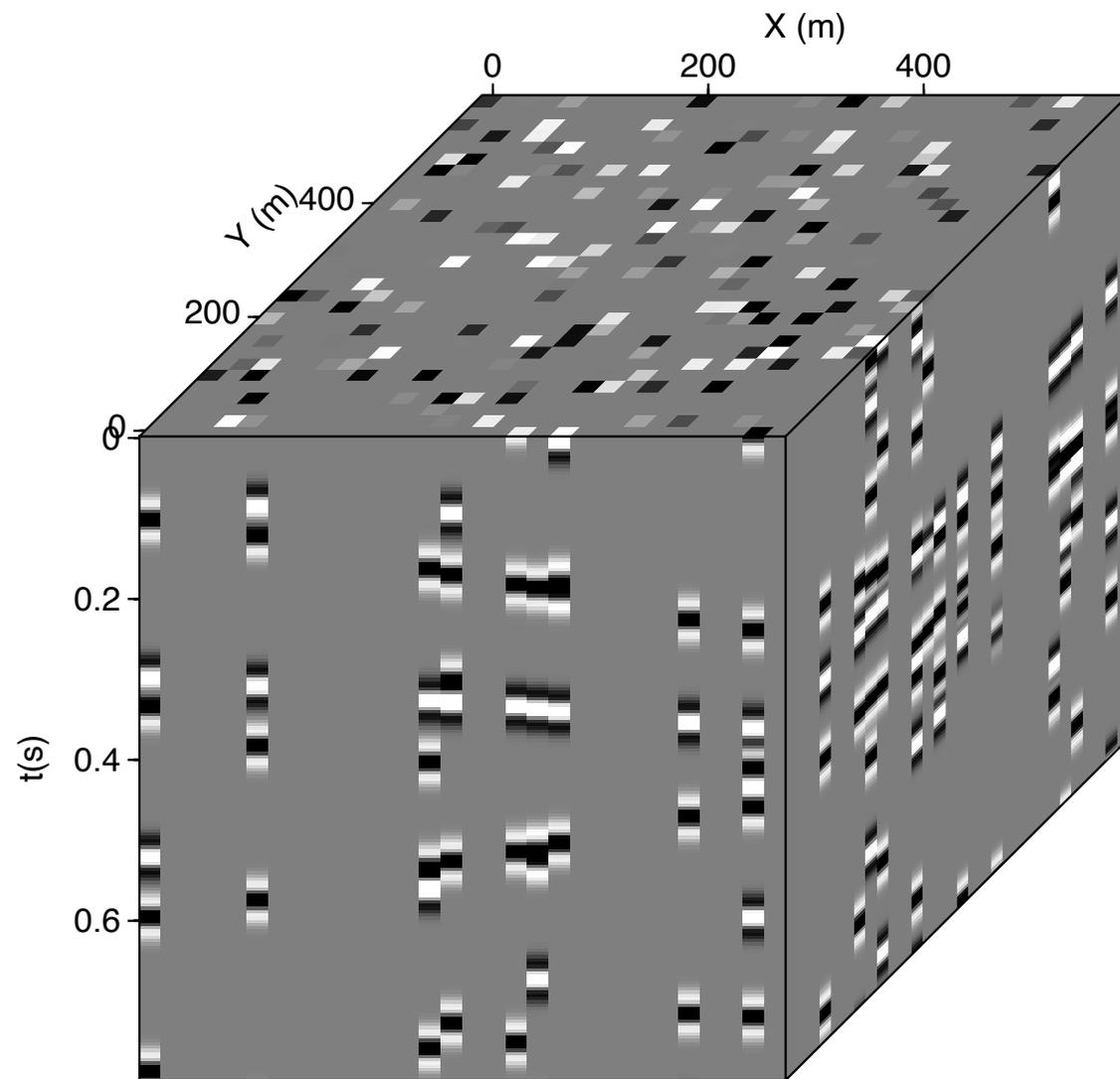
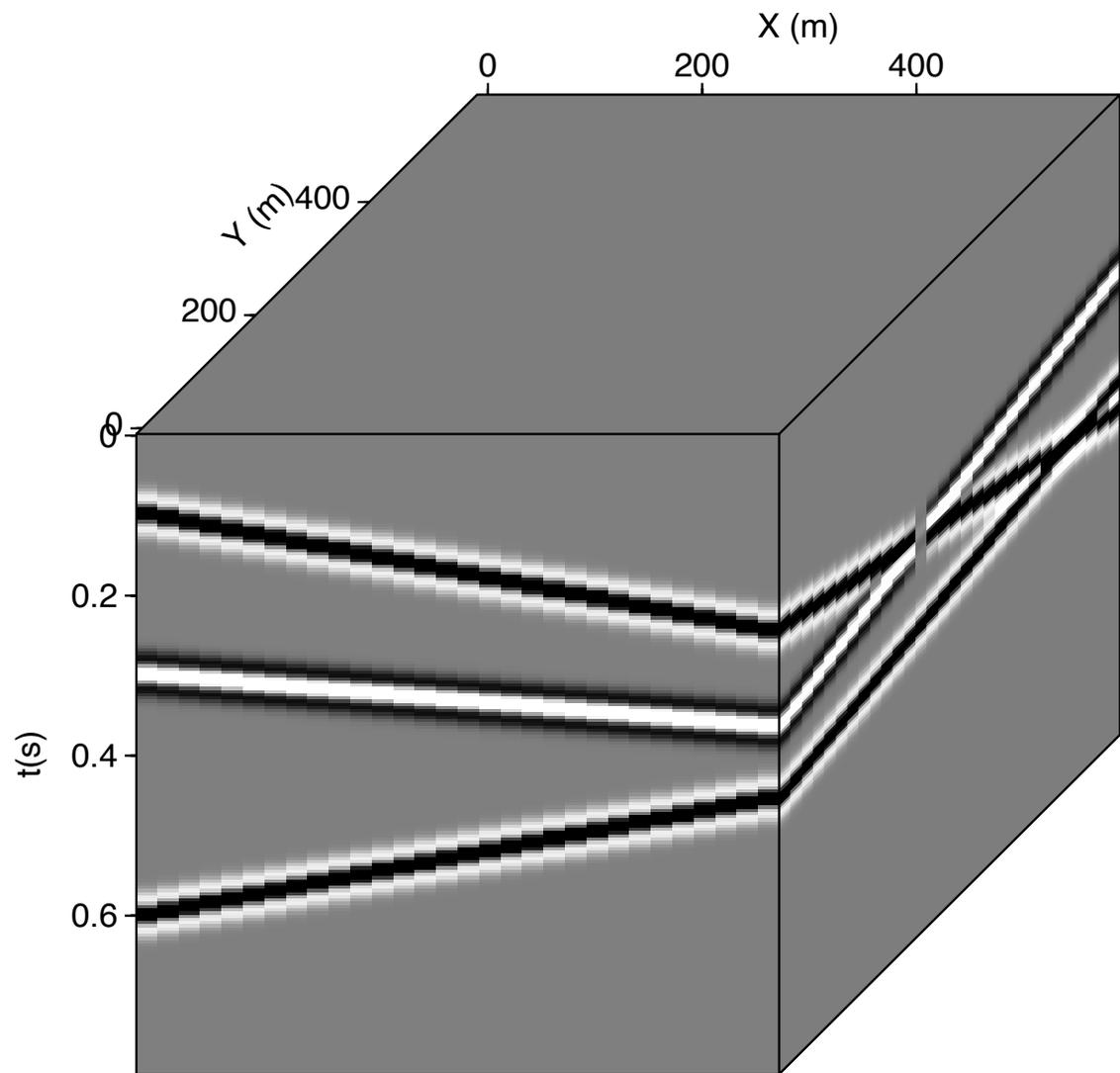


MSSA + Binning

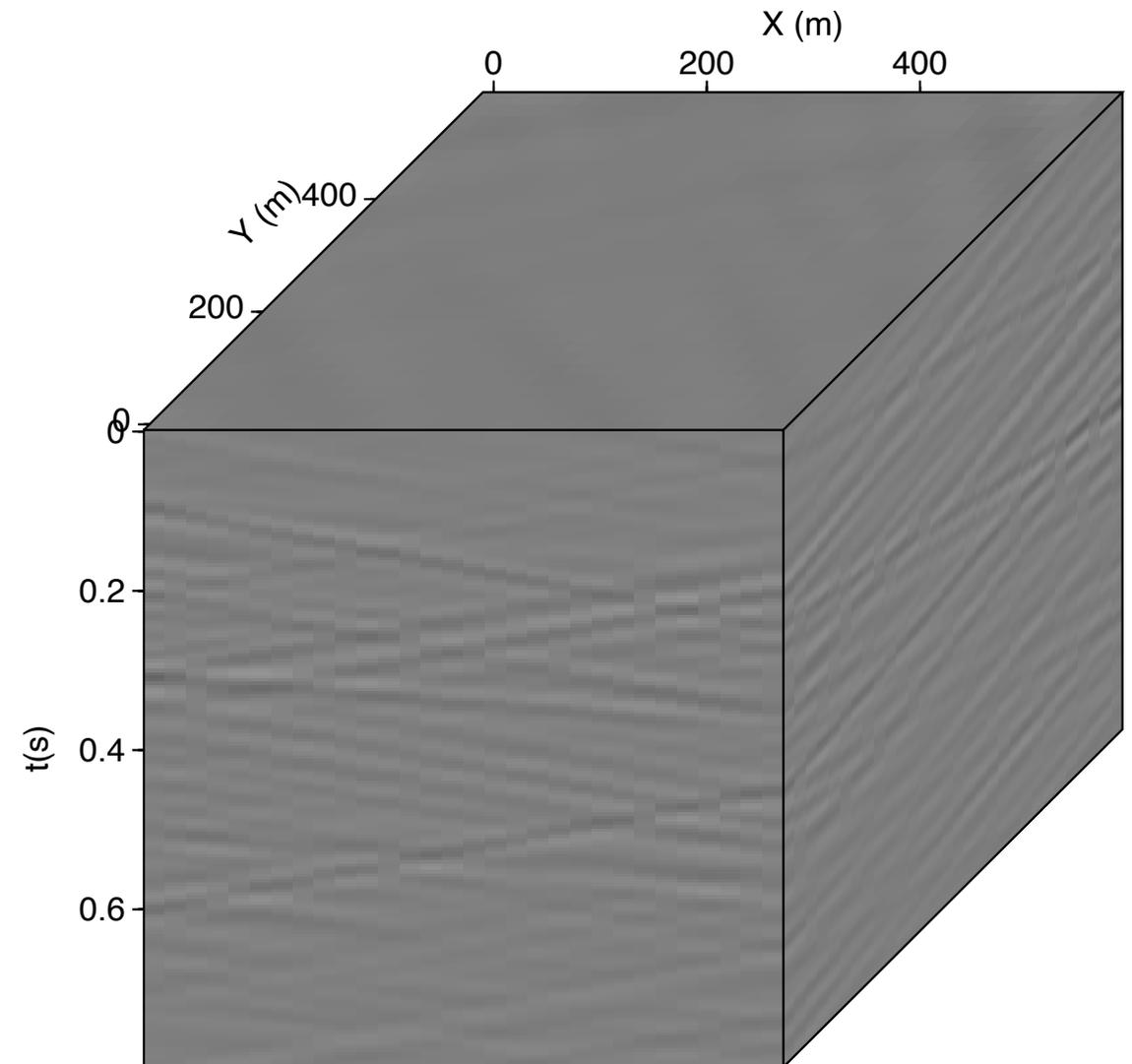
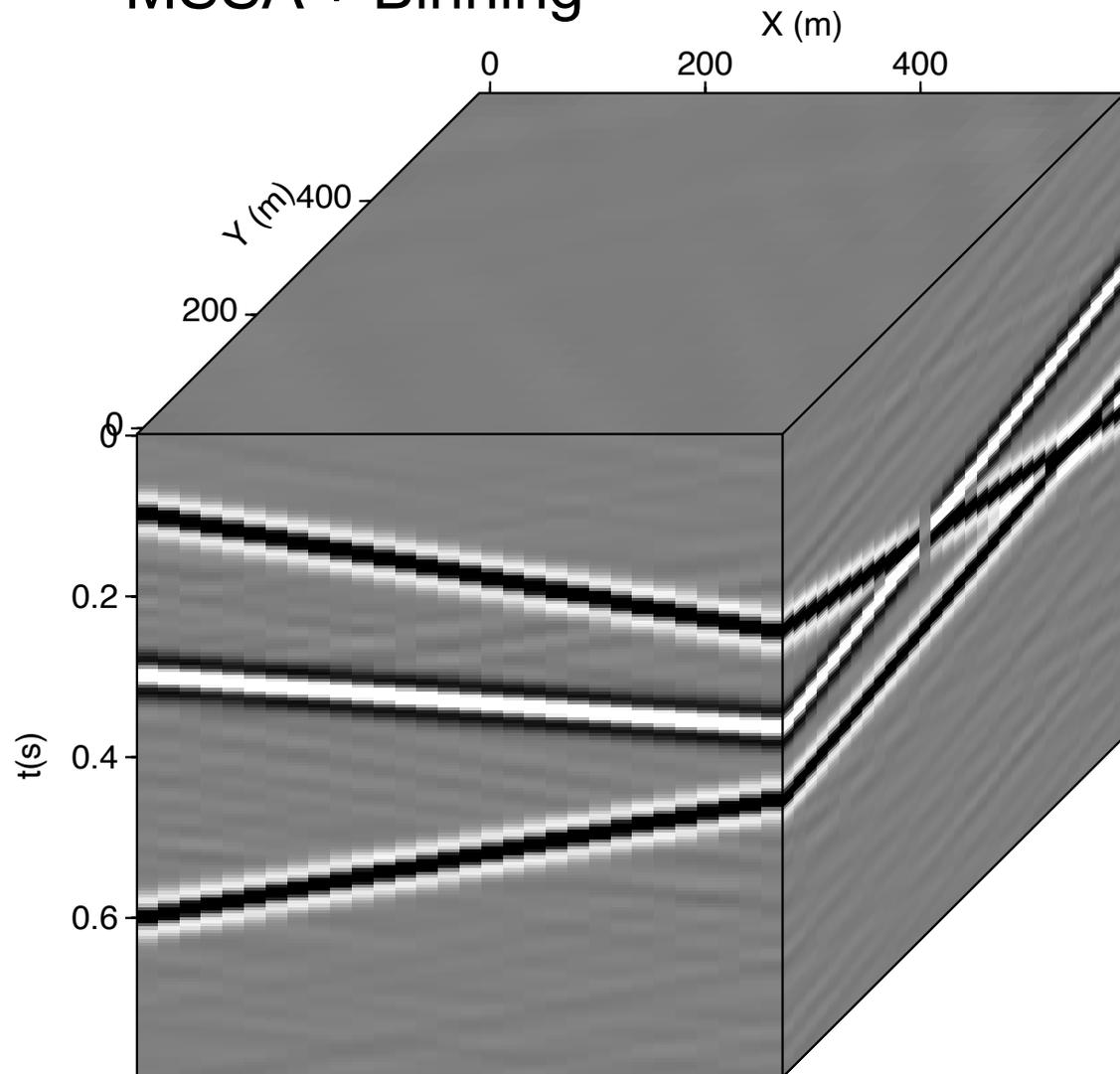


I-MSSA

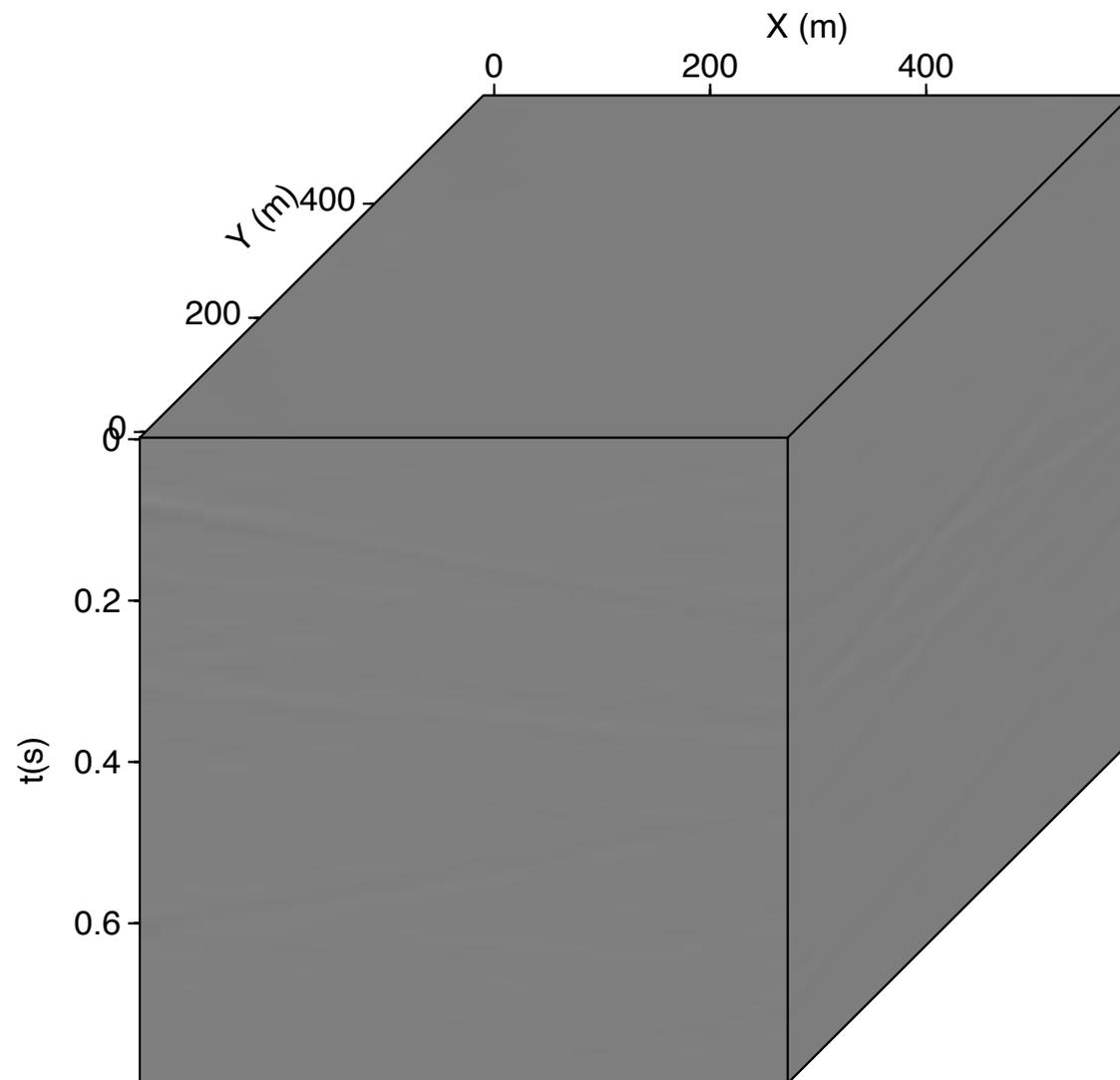
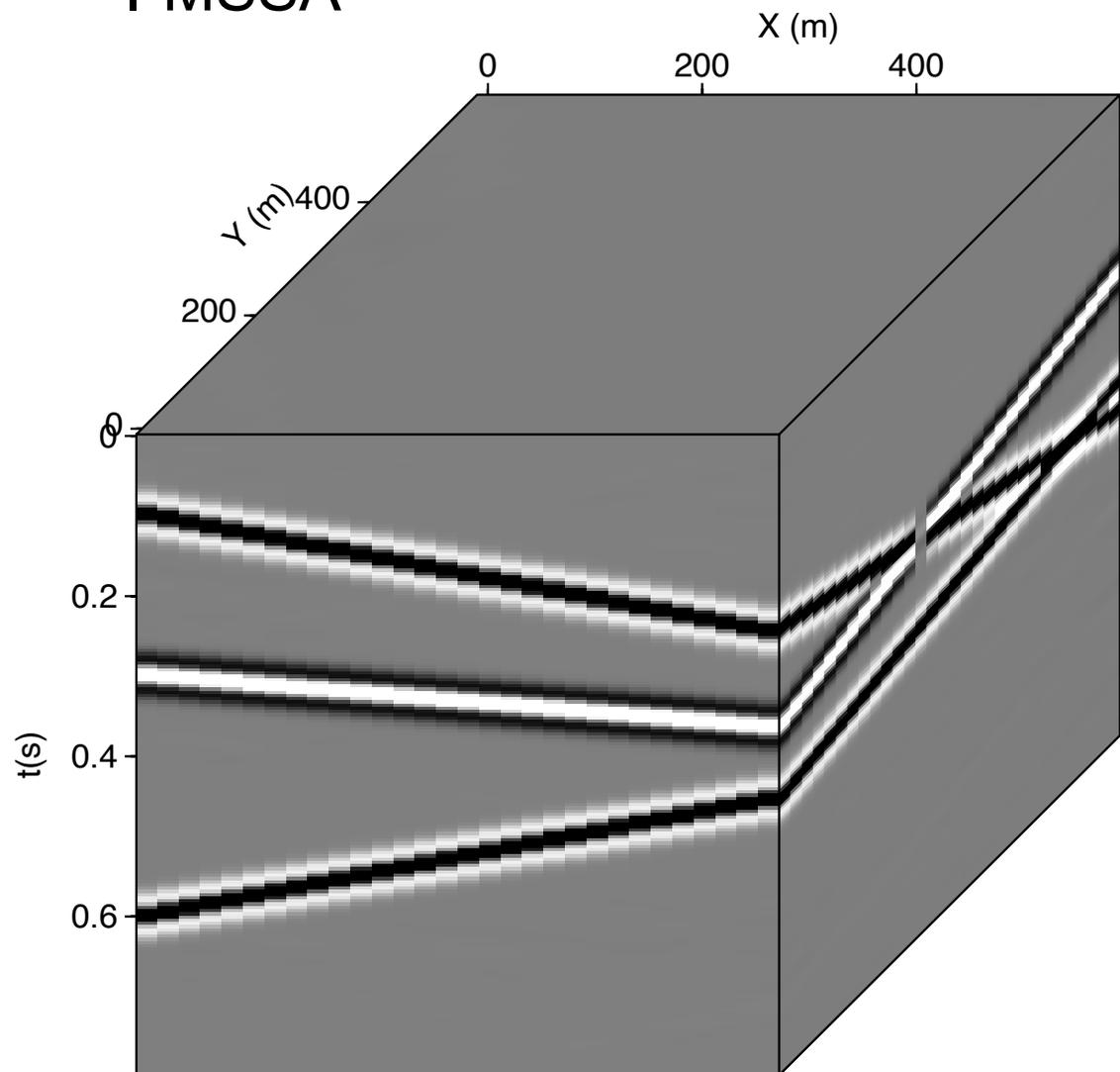




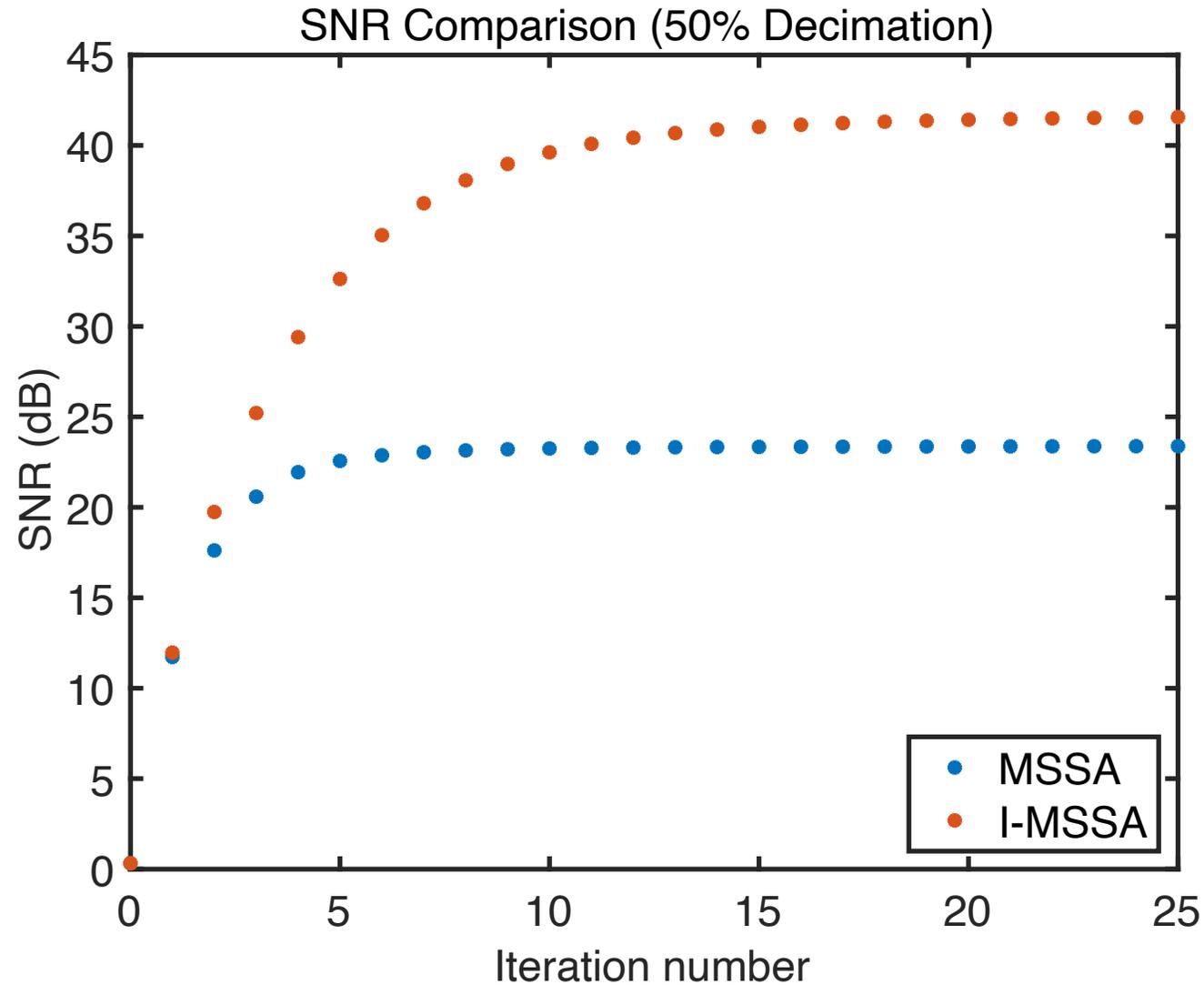
MSSA + Binning



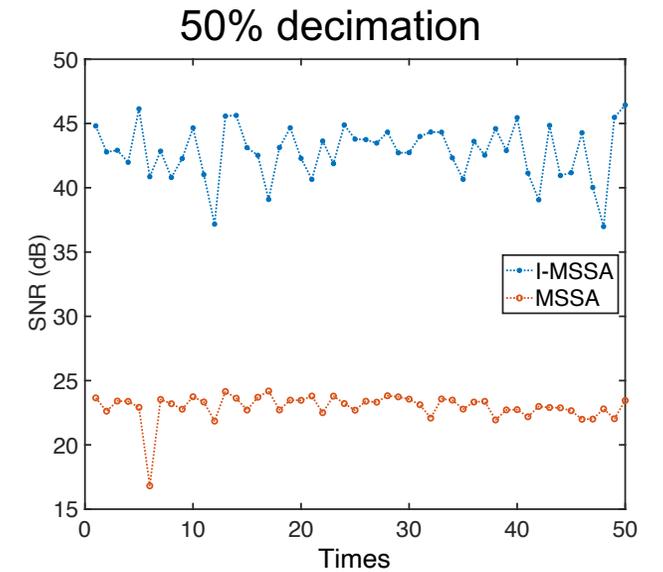
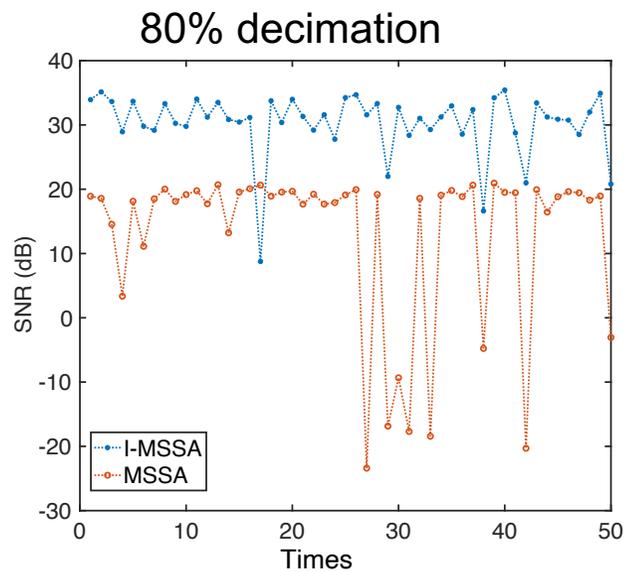
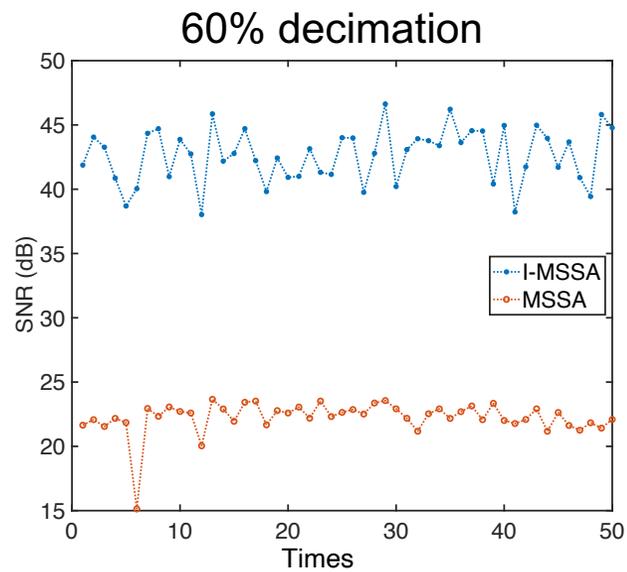
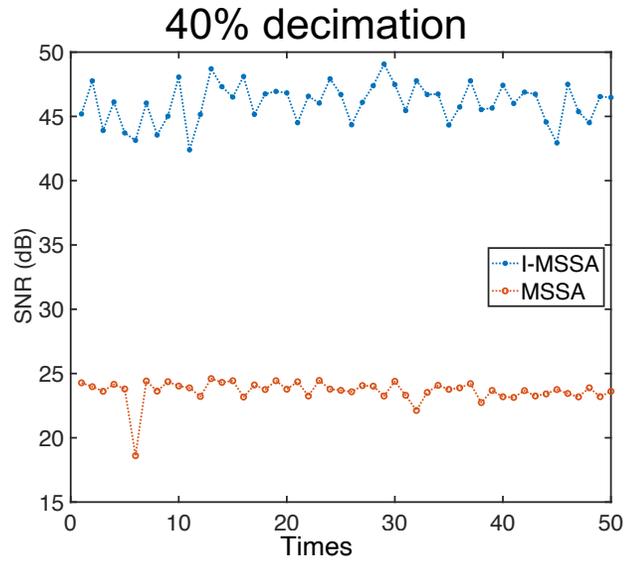
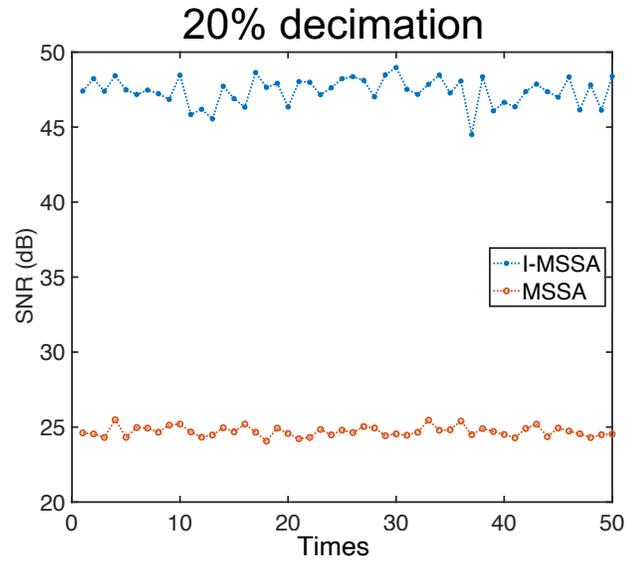
## I-MSSA



50% decimation

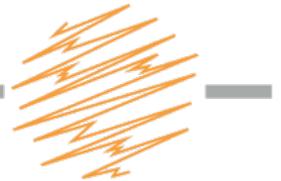


50 times random schemes

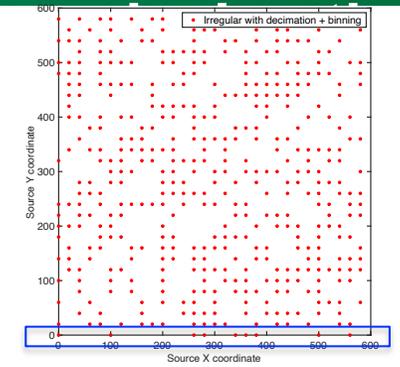
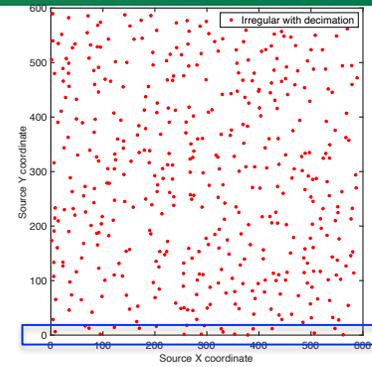
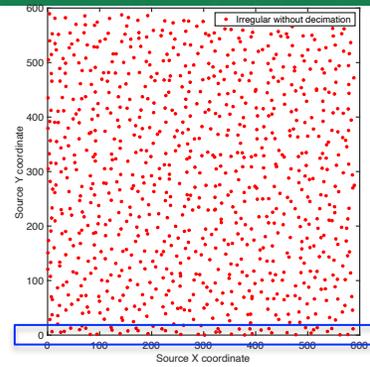
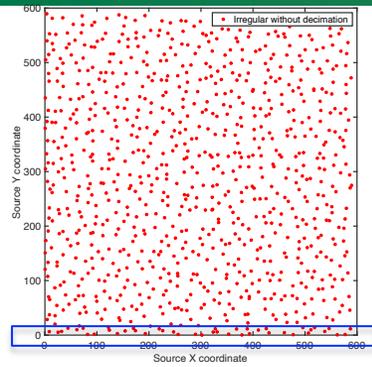
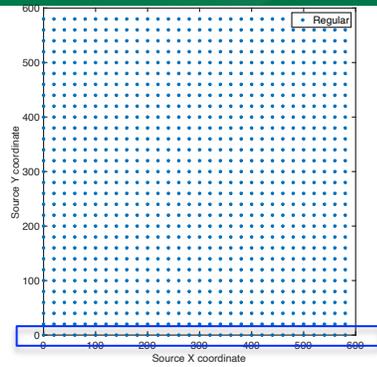


Gaussian Noise (SNR=1) + Blending noise (BF=2) + 50% decimation

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# Gaussian Noise (SNR=2) + Blending noise (BF=2) + 50%



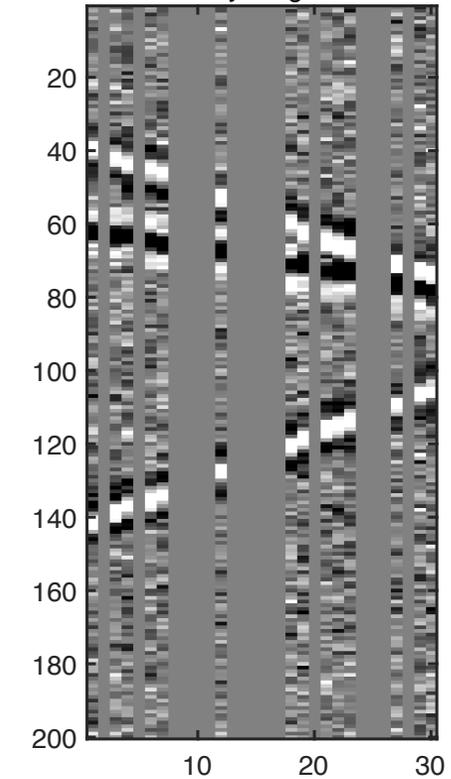
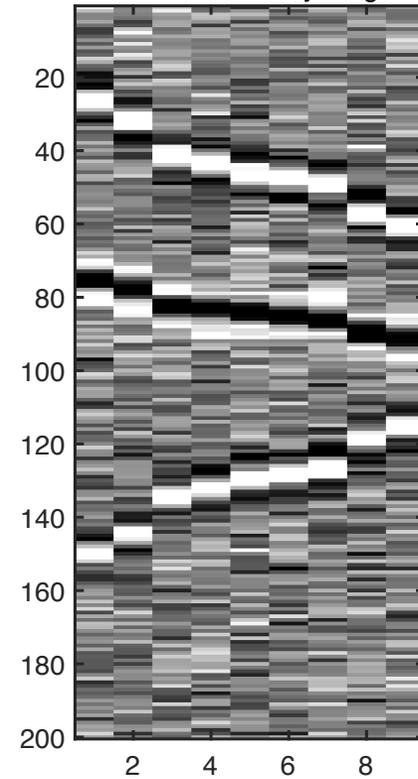
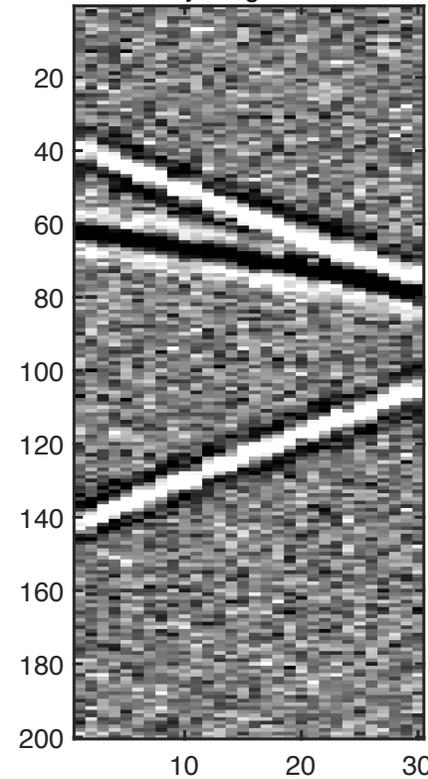
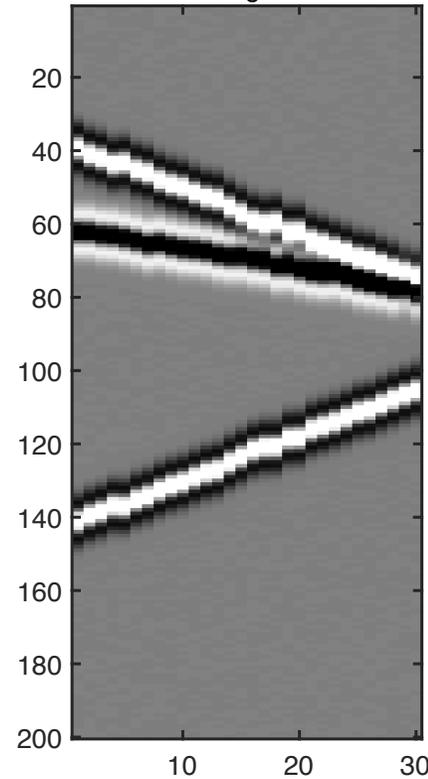
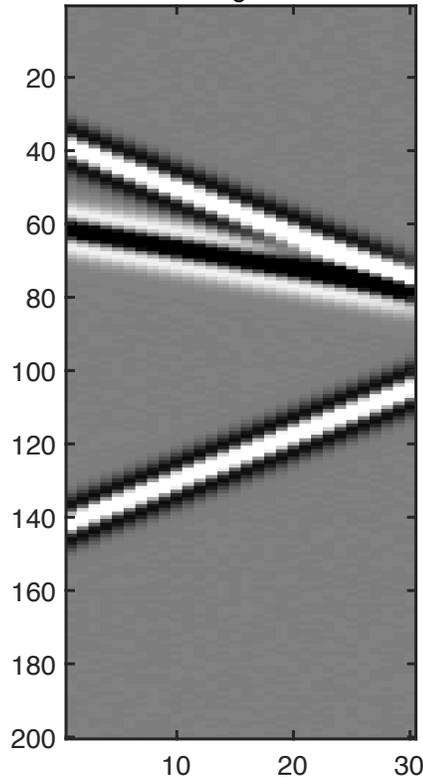
Clean regular data

Clean irregular data

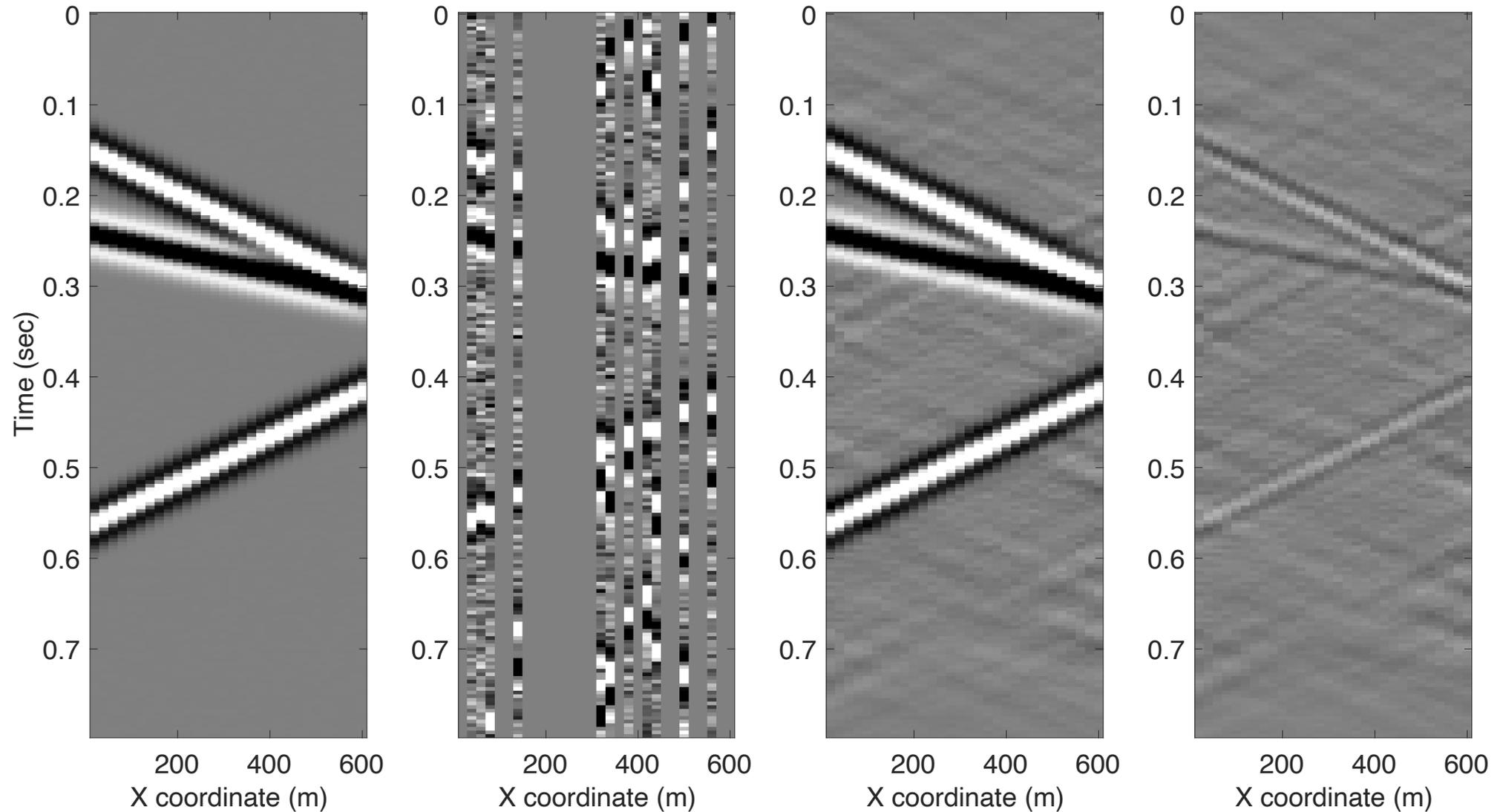
Noisy irregular data

Observed real noisy irregular

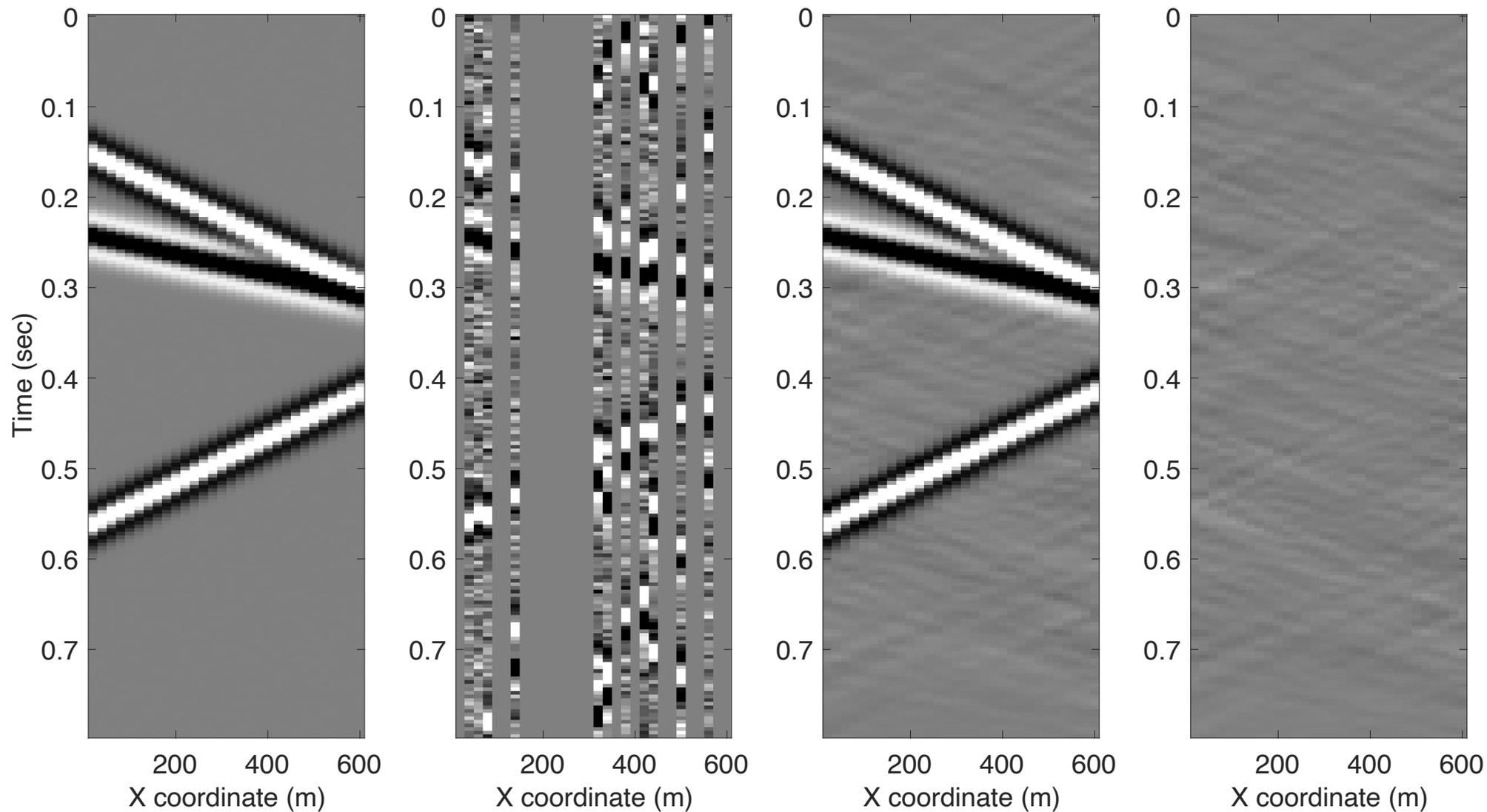
Observed noisy irregular + binning

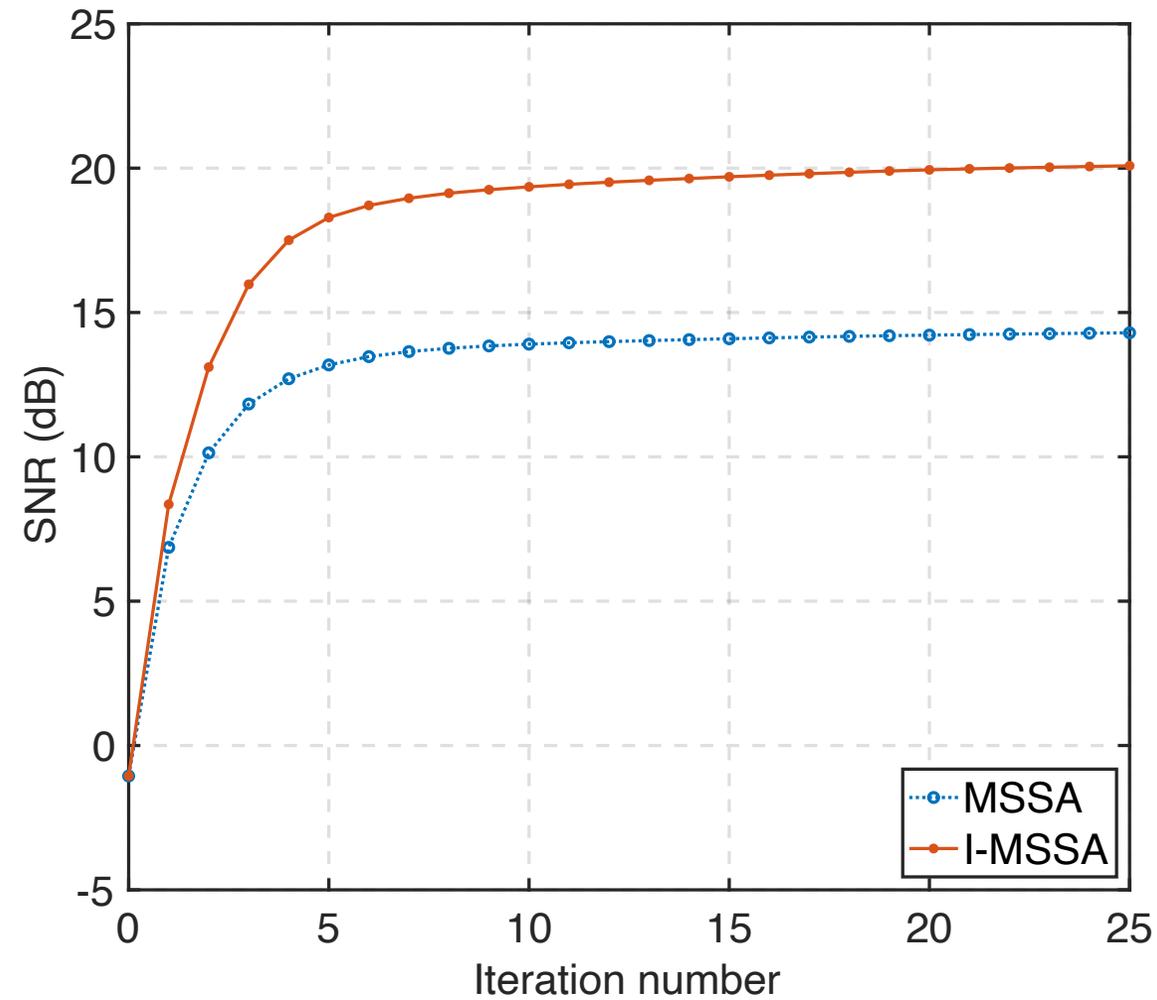


## Synthetic example (Deblending + MSSA reconstruction)

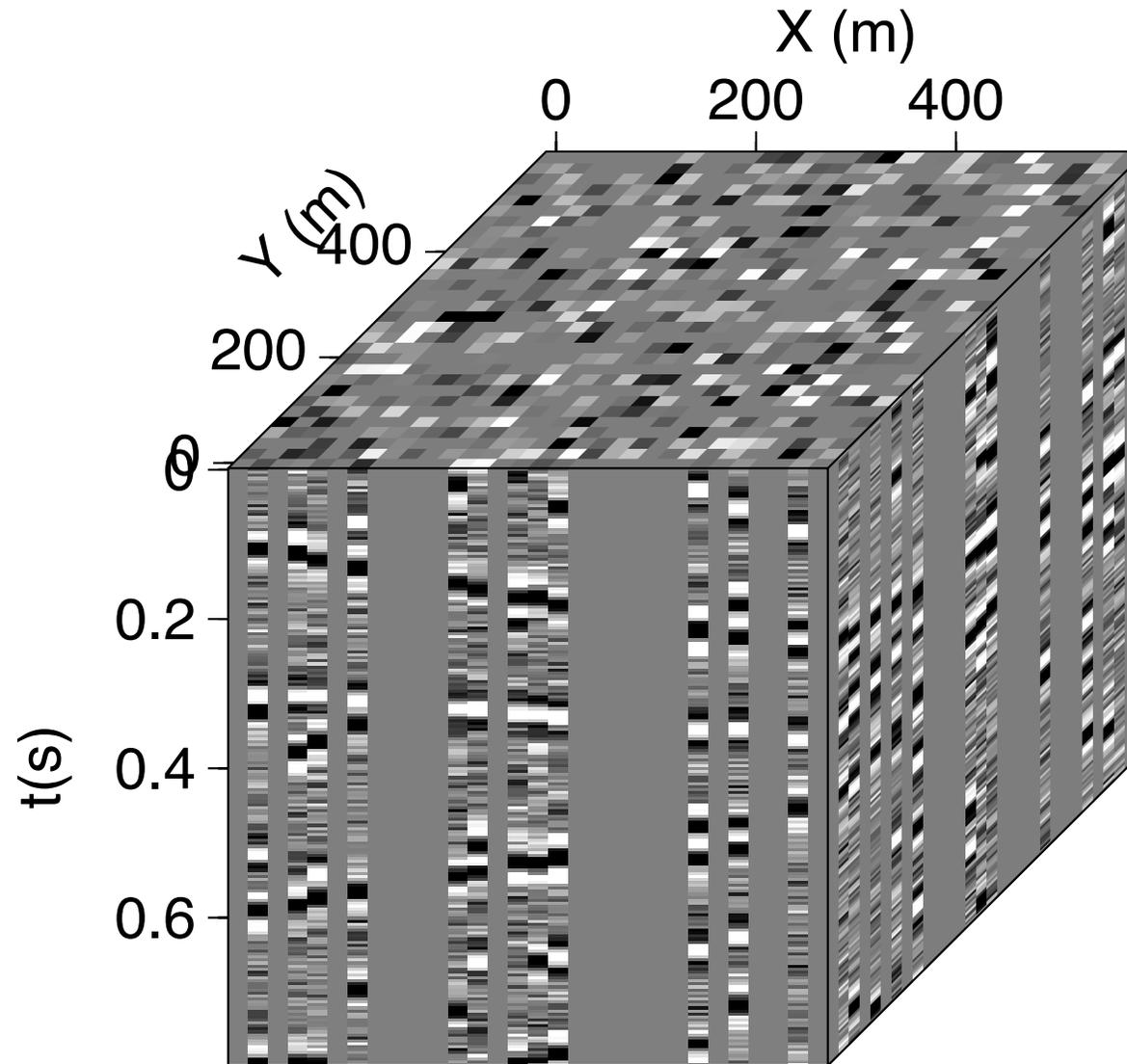


### Synthetic example (Deblending + I-MSSA reconstruction)

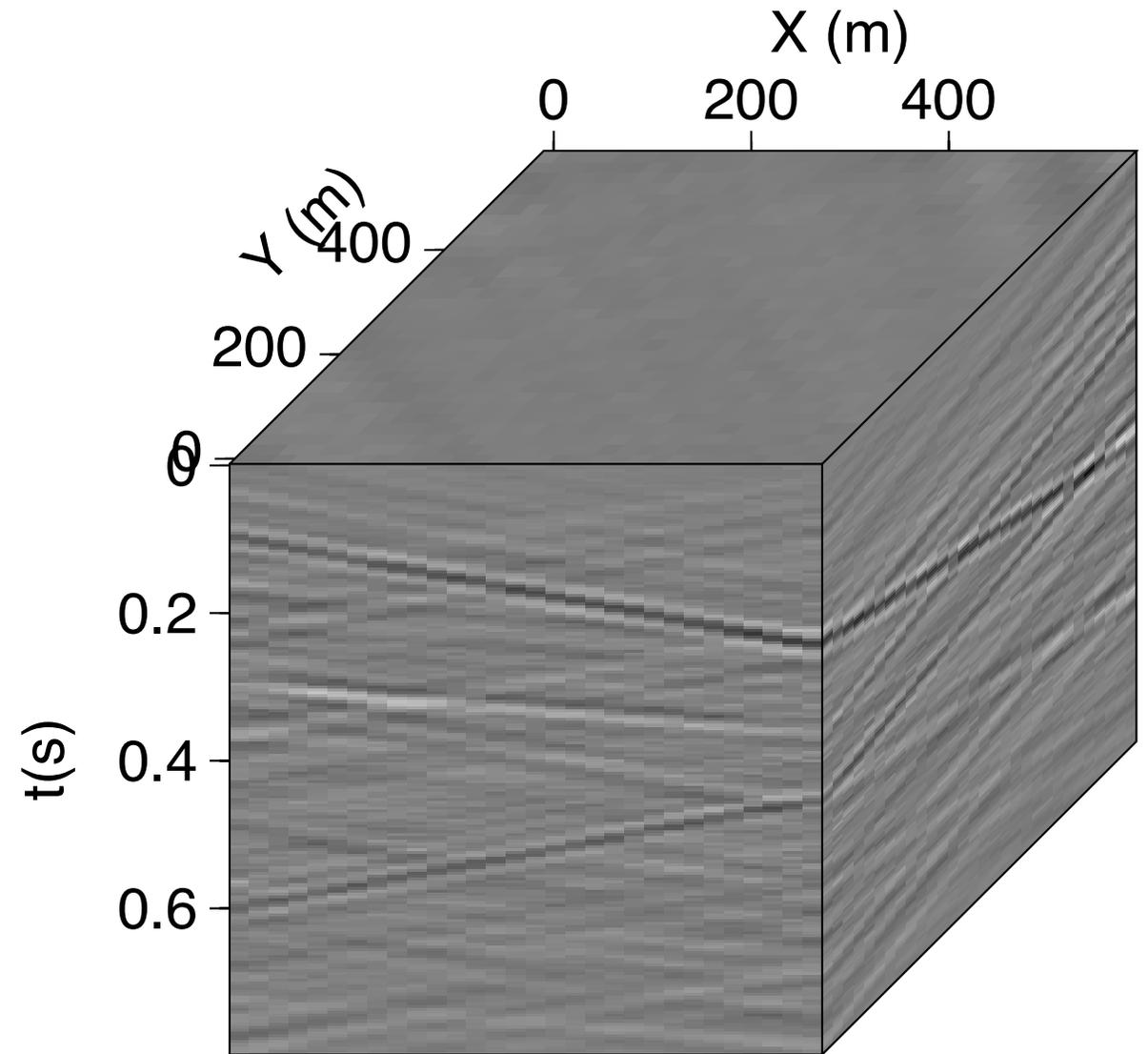
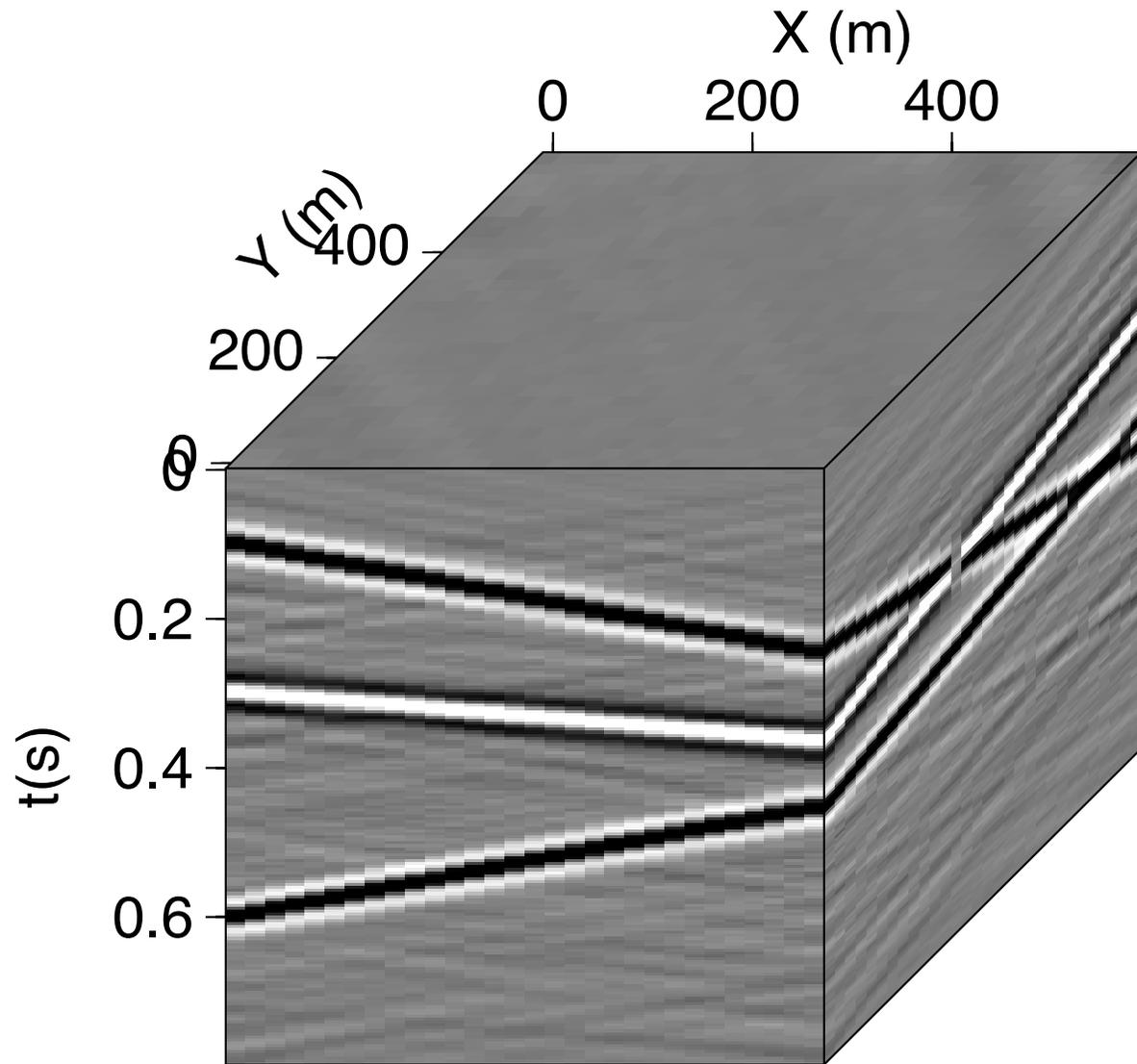




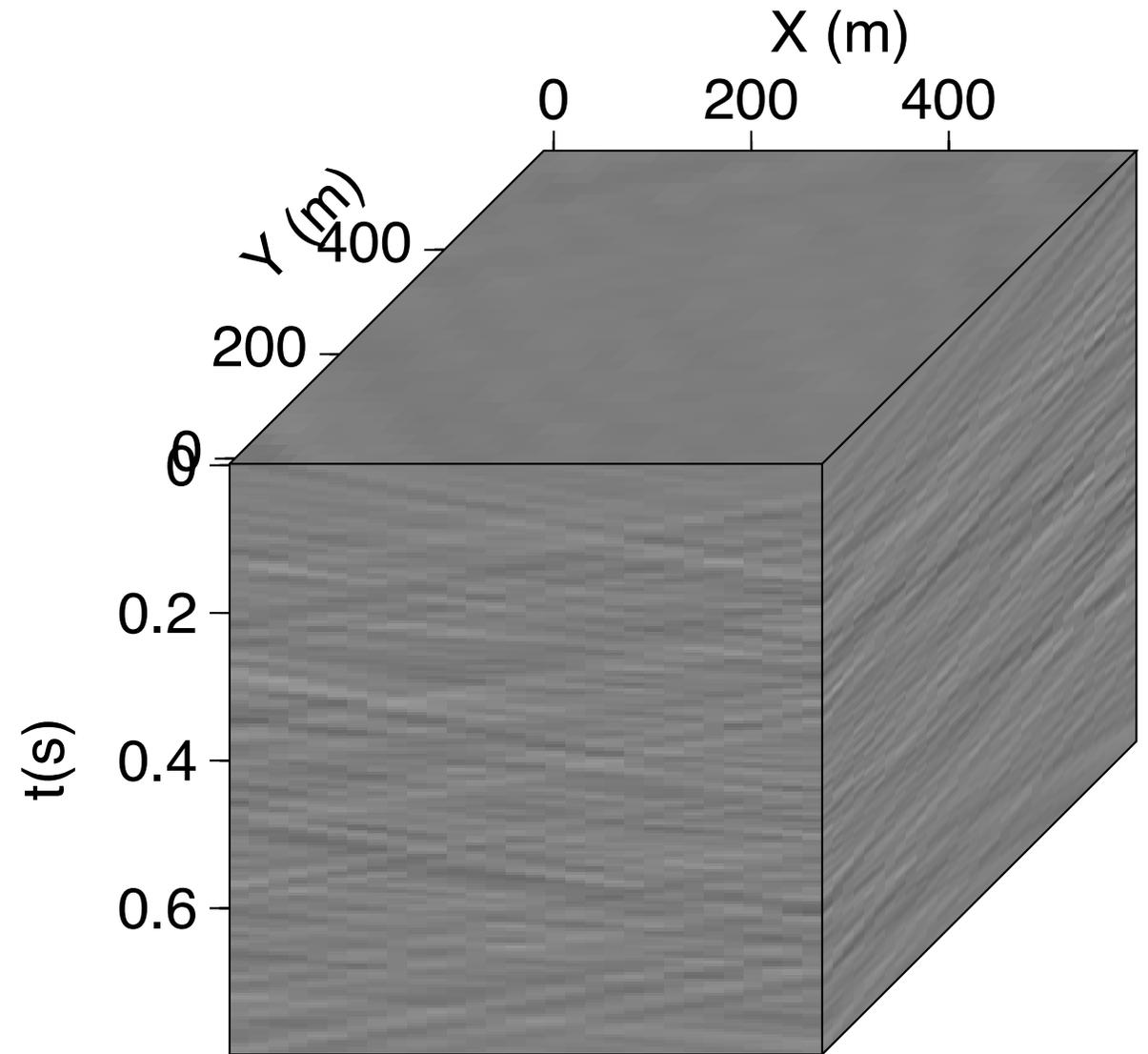
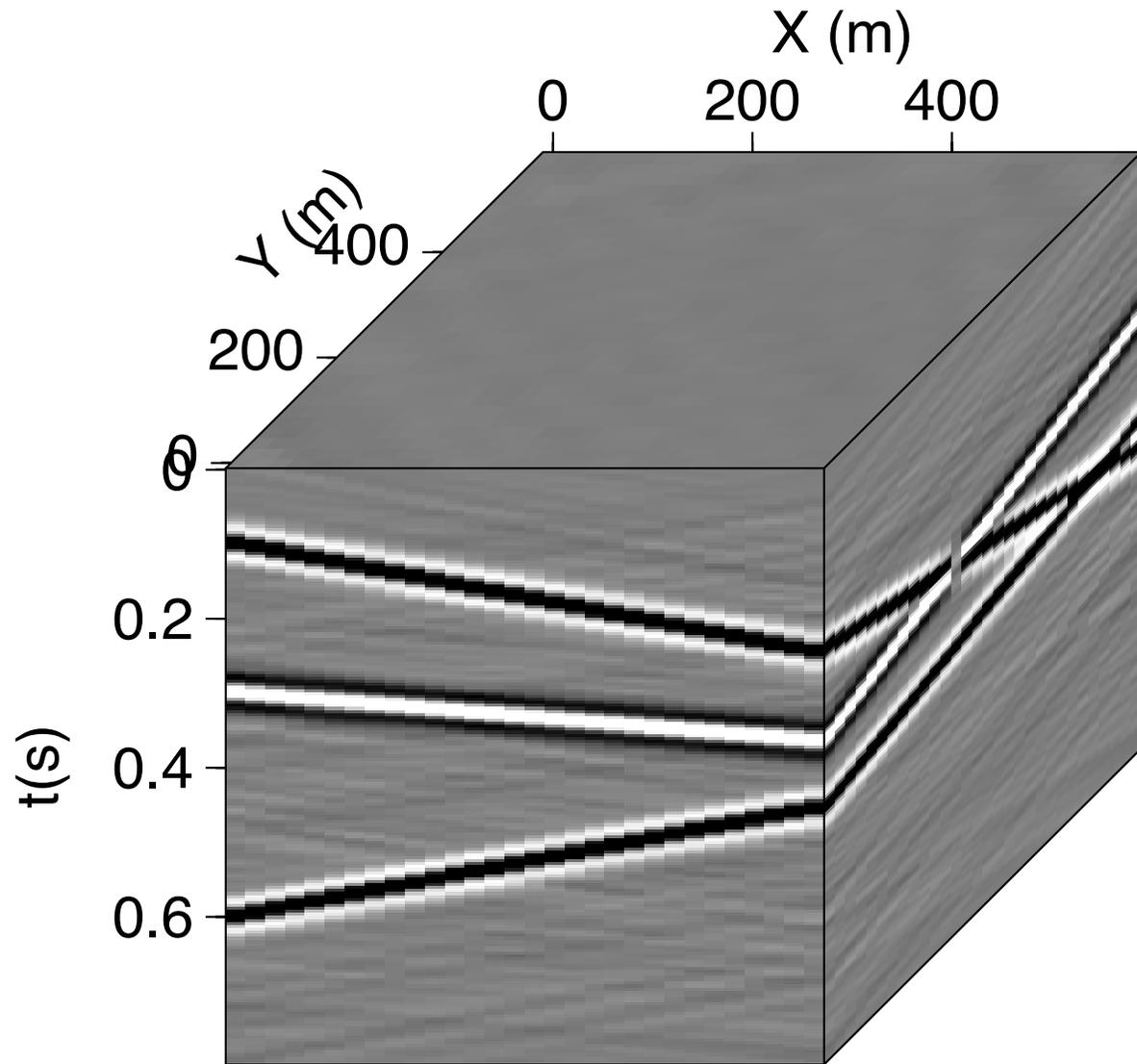
Synthetic example (Deblending + I-MSSA reconstruction)



Synthetic example (Deblending + MSSA reconstruction)



Synthetic example (Deblending + I-MSSA reconstruction)

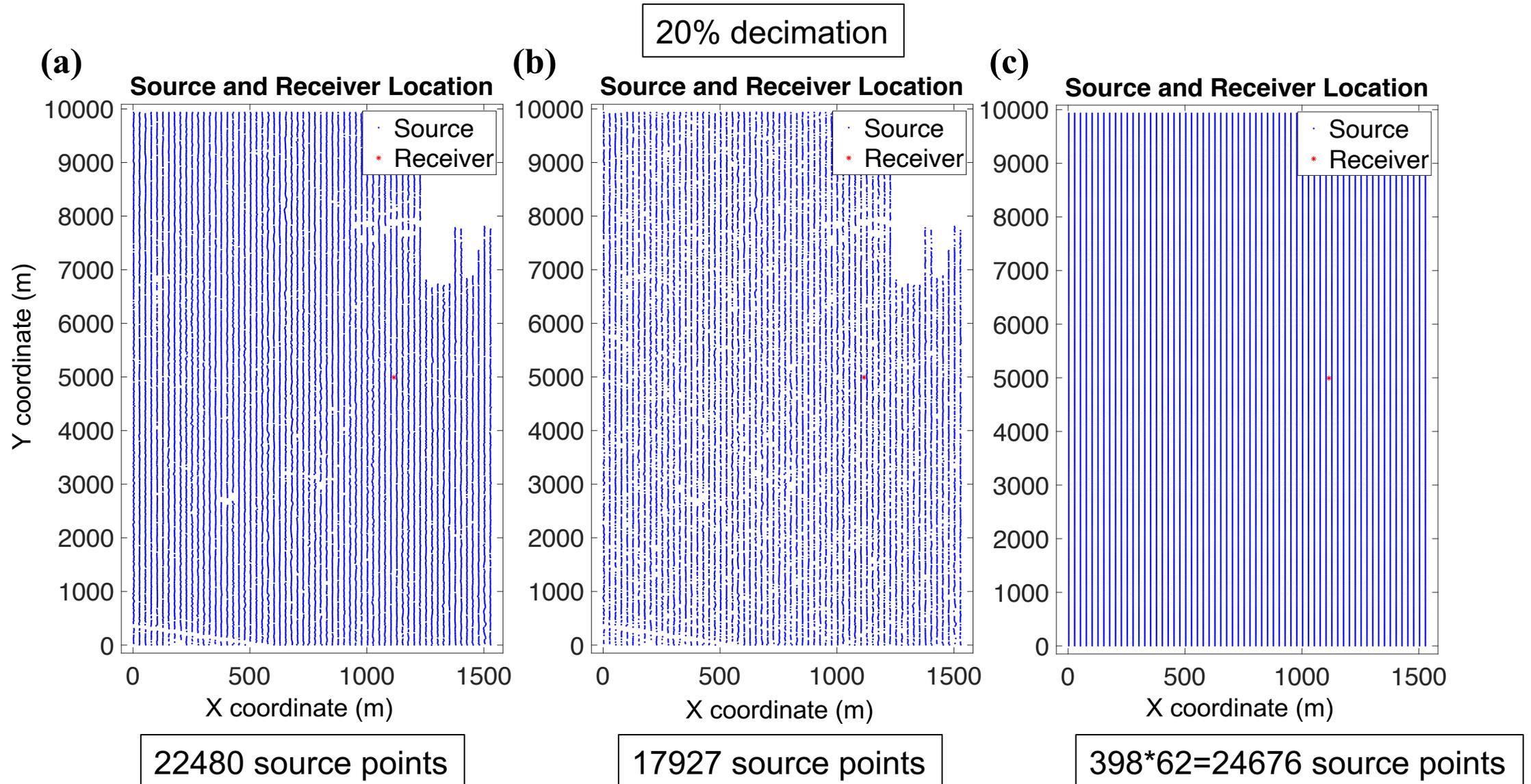


# Real Example (Deblending + Irregular Reconstruction)

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- Coordinate distribution





$$J = \|\mathbf{b} - \mathcal{B}\mathcal{W}\mathbf{D}\|_2^2 \quad \text{s.t.} \quad \text{rank}(\mathbf{D}) \leq k$$



$$J = \|\mathbf{b} - \mathcal{B}\mathcal{W}\mathcal{L}\mathbf{D}\|_2^2 \quad \text{s.t.} \quad \text{rank}(\mathbf{D}) \leq k$$

$\mathcal{L}$  : Unpatch operator       $\mathcal{W}$  : regular  $\rightarrow$  irregular

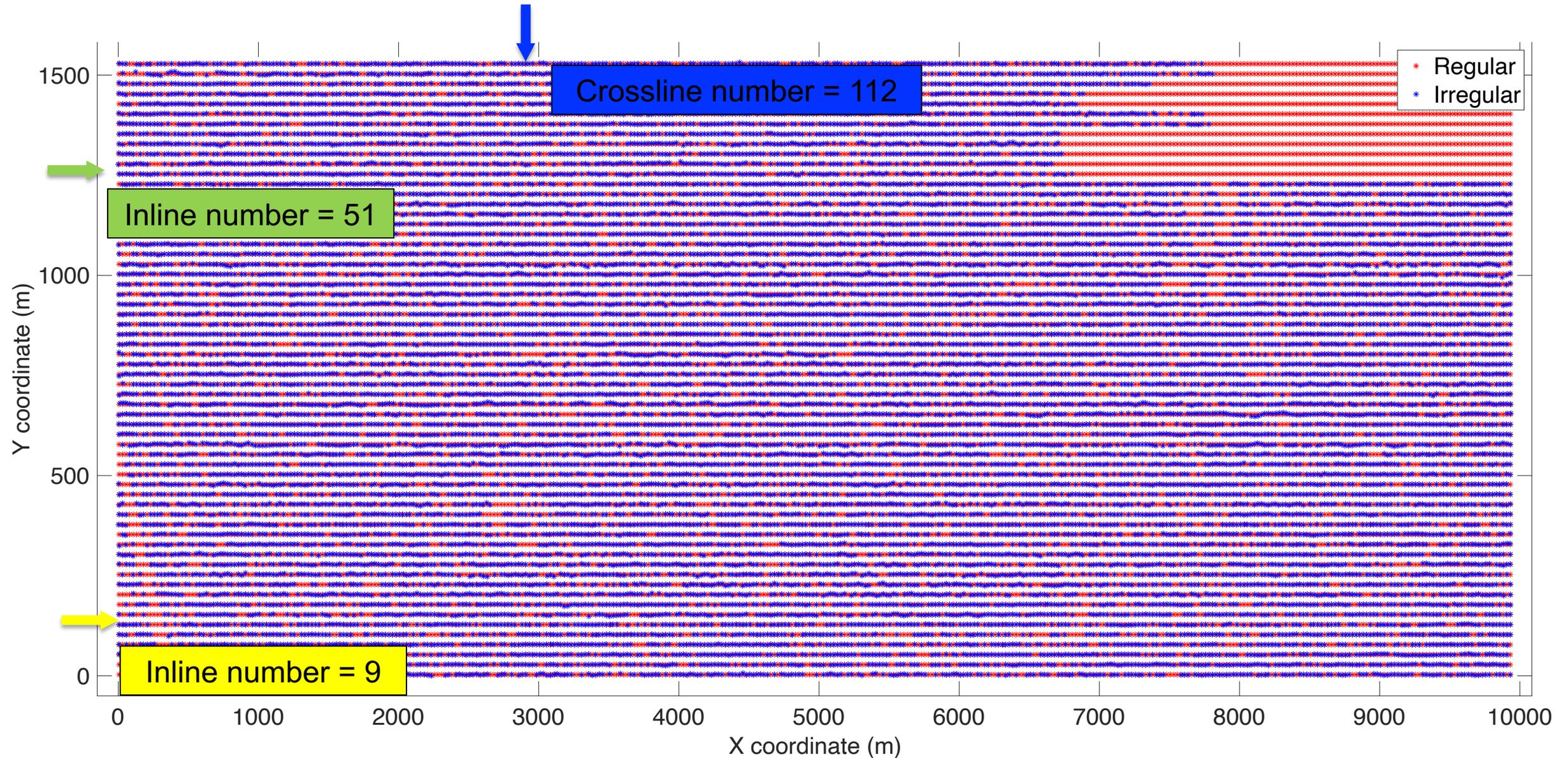
$\mathcal{L}^*$  : Patch operator       $\mathcal{W}^*$  : irregular  $\rightarrow$  regular

• *Sinc-Kaiser interpolator*

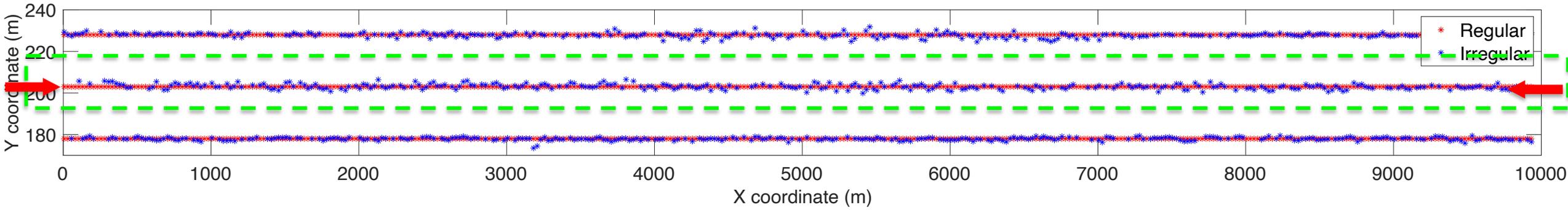
$$\mathbf{D}^\nu = \mathcal{L}\mathcal{P}\mathcal{L}^*[\mathbf{D}^{\nu-1} - \lambda\mathcal{W}^*\mathcal{B}^*(\mathcal{B}\mathcal{W}\mathbf{D}^{\nu-1} - \mathbf{b})]$$



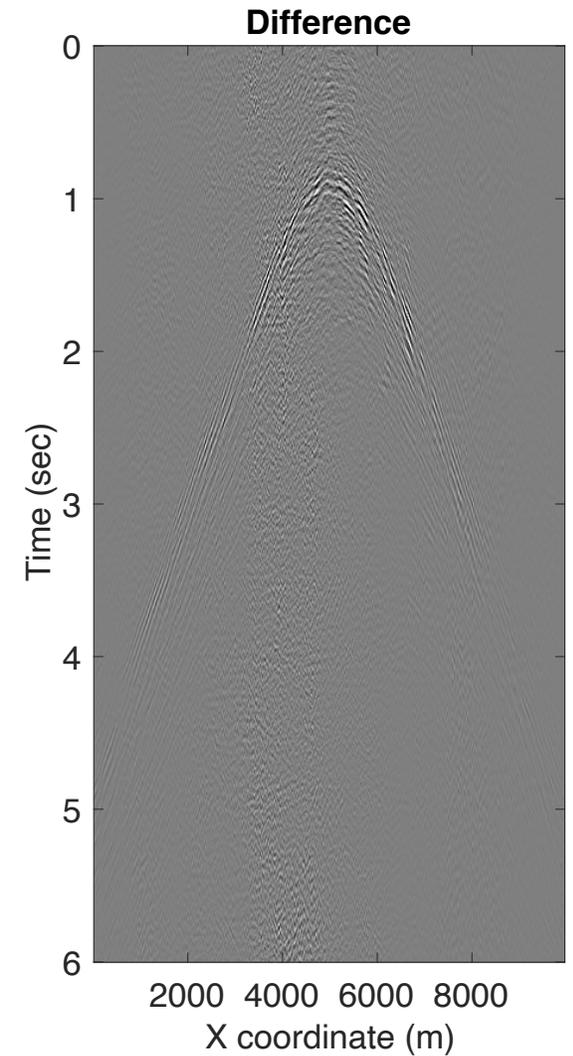
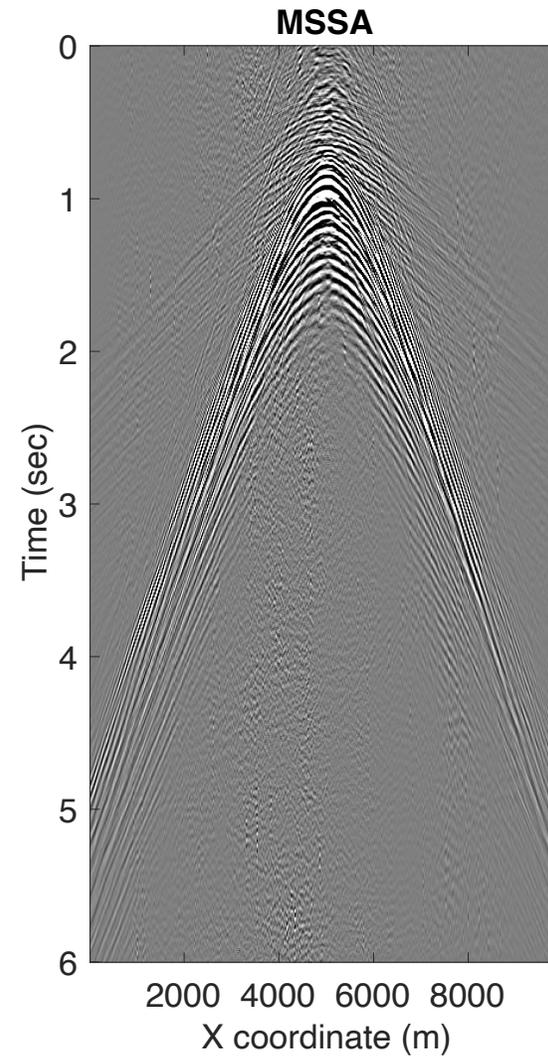
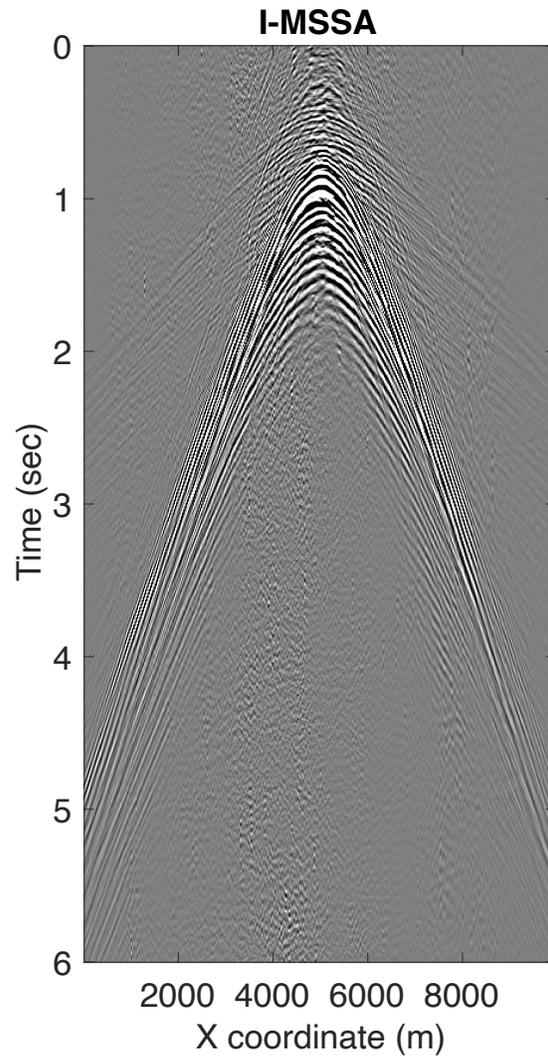
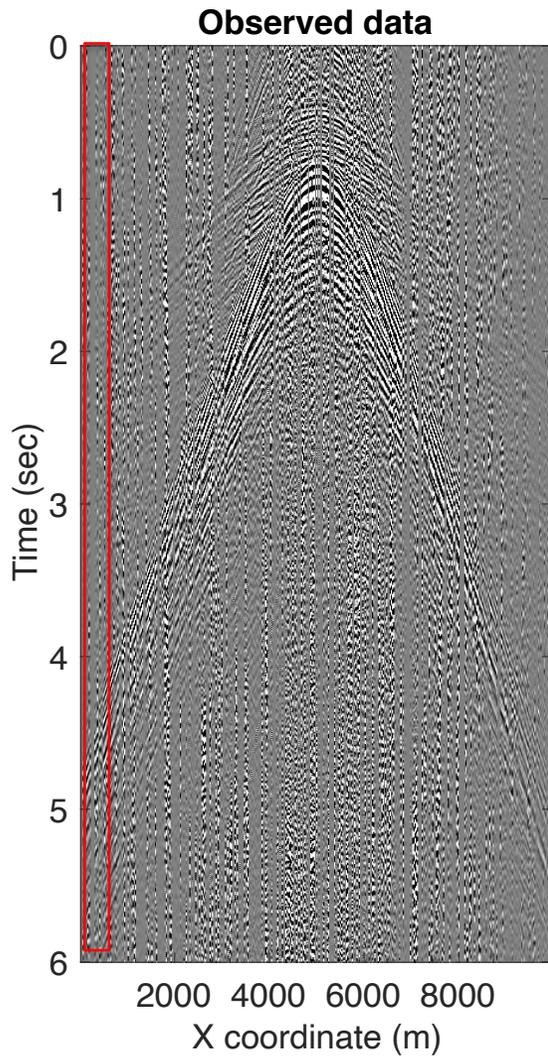
*Projection operator = MSSA*



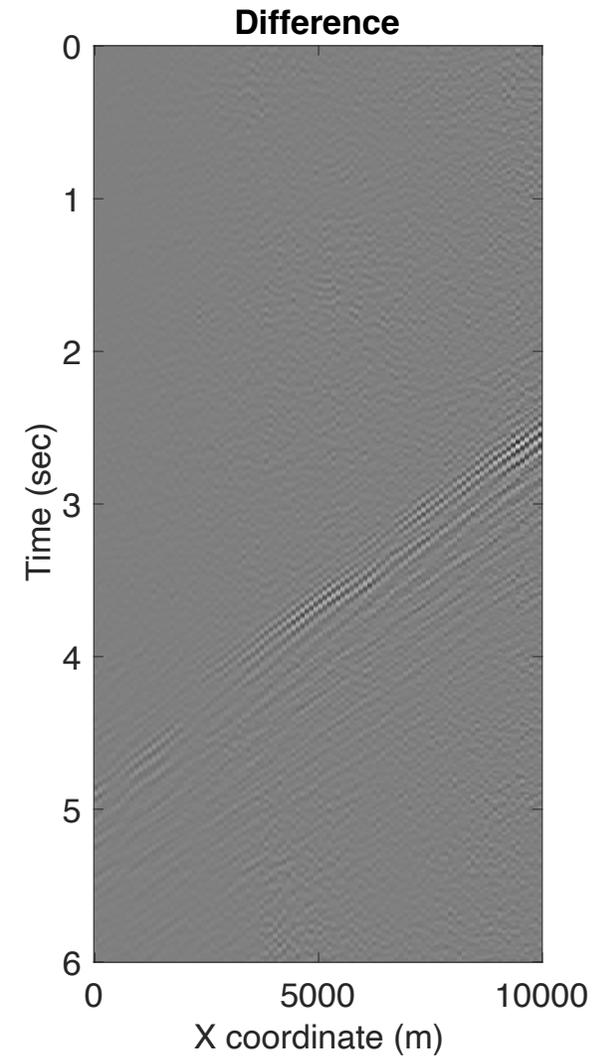
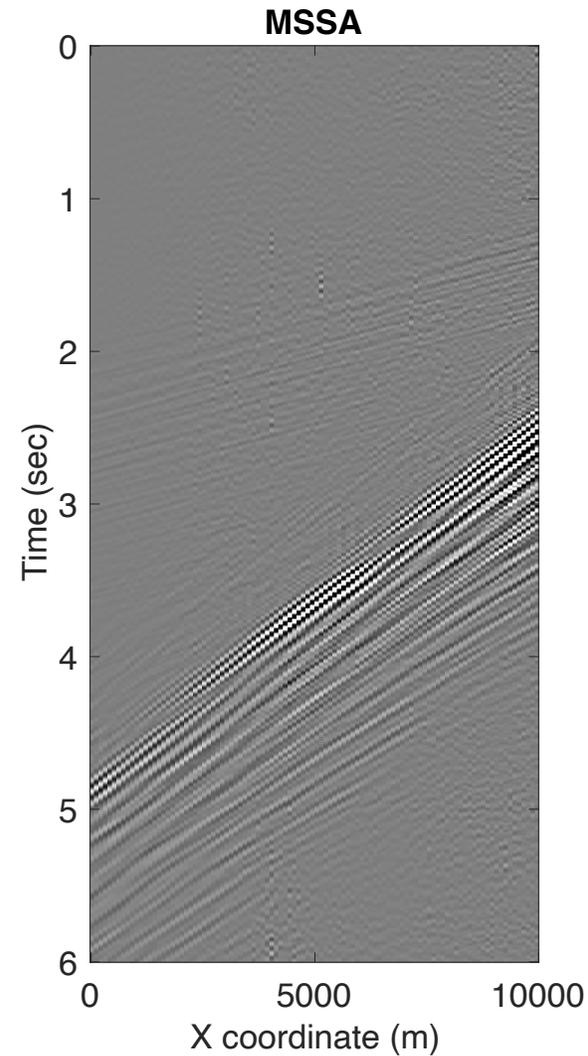
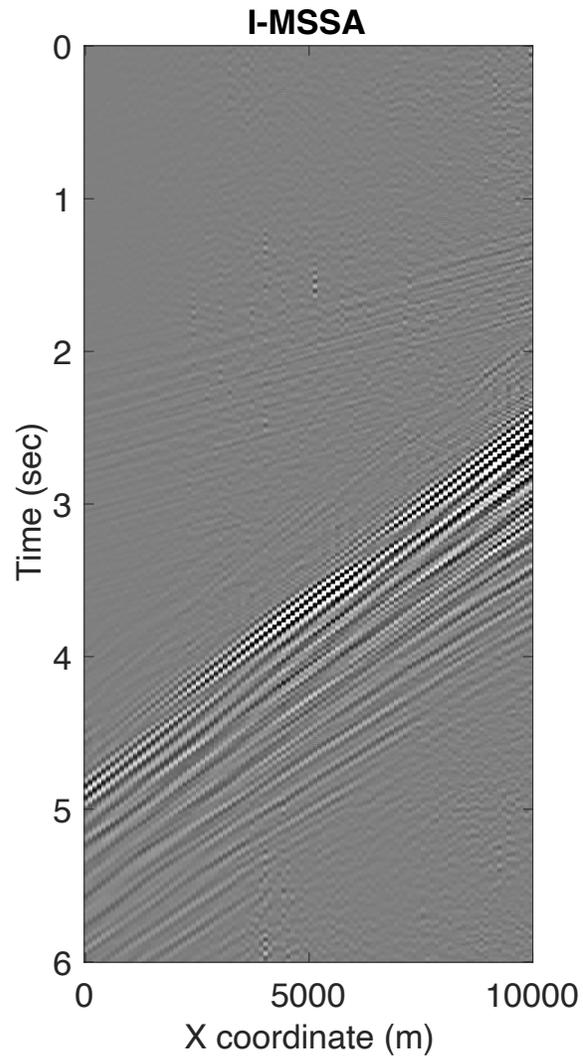
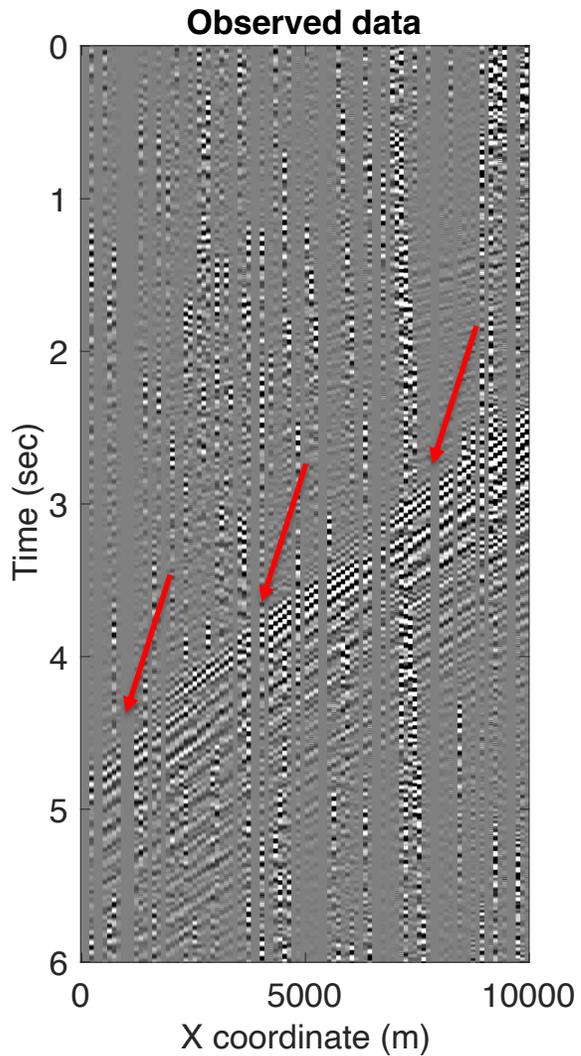
Inline number = 9



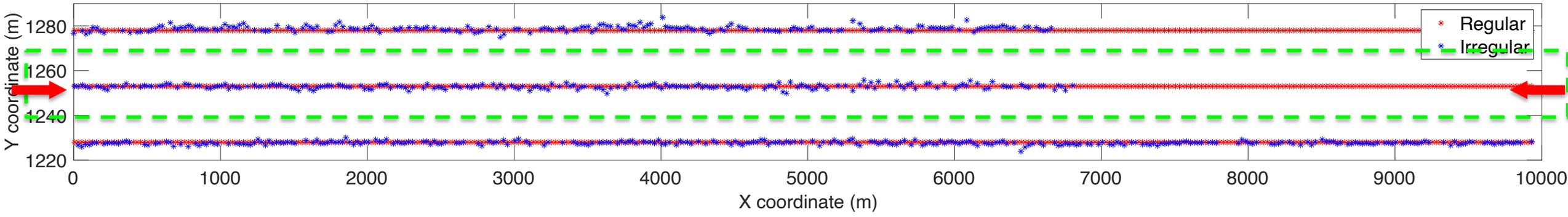
- Inline number = 9



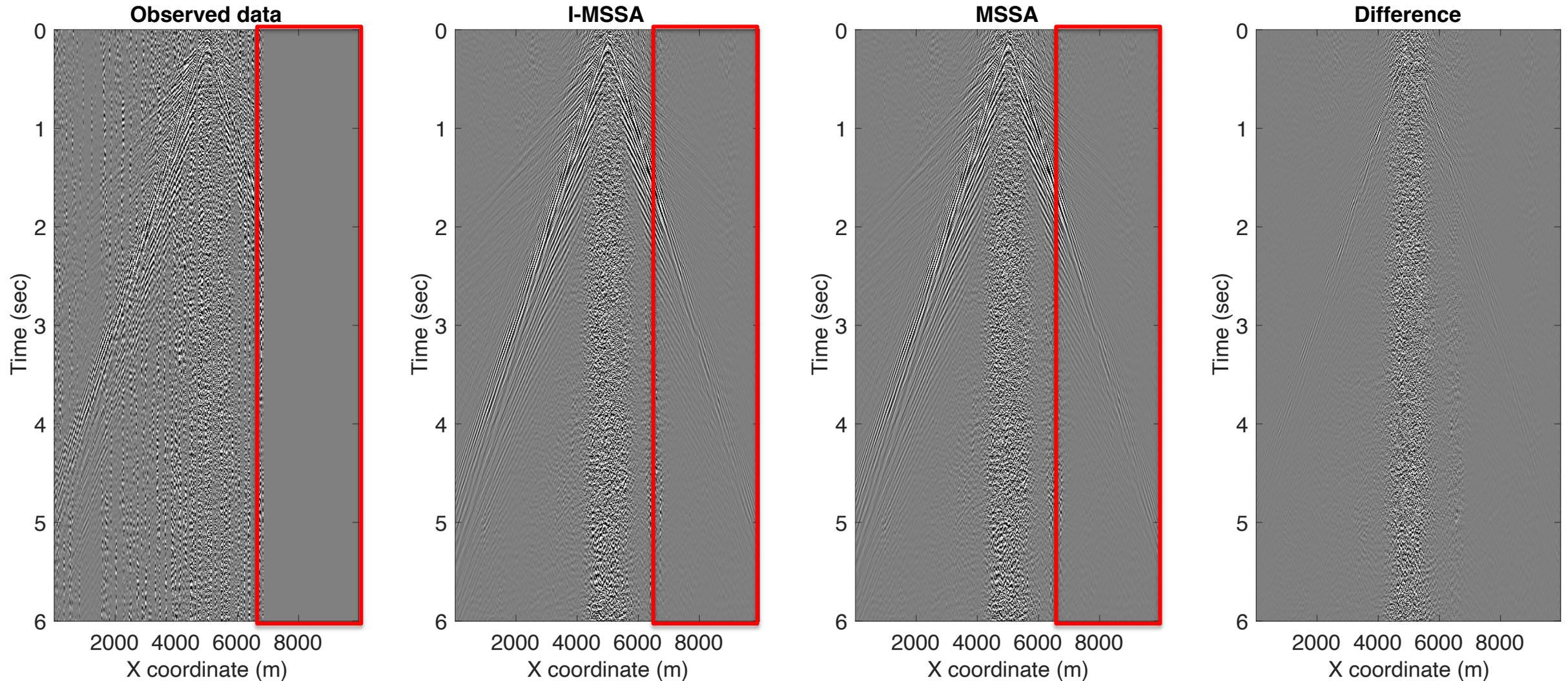
- Inline number = 9



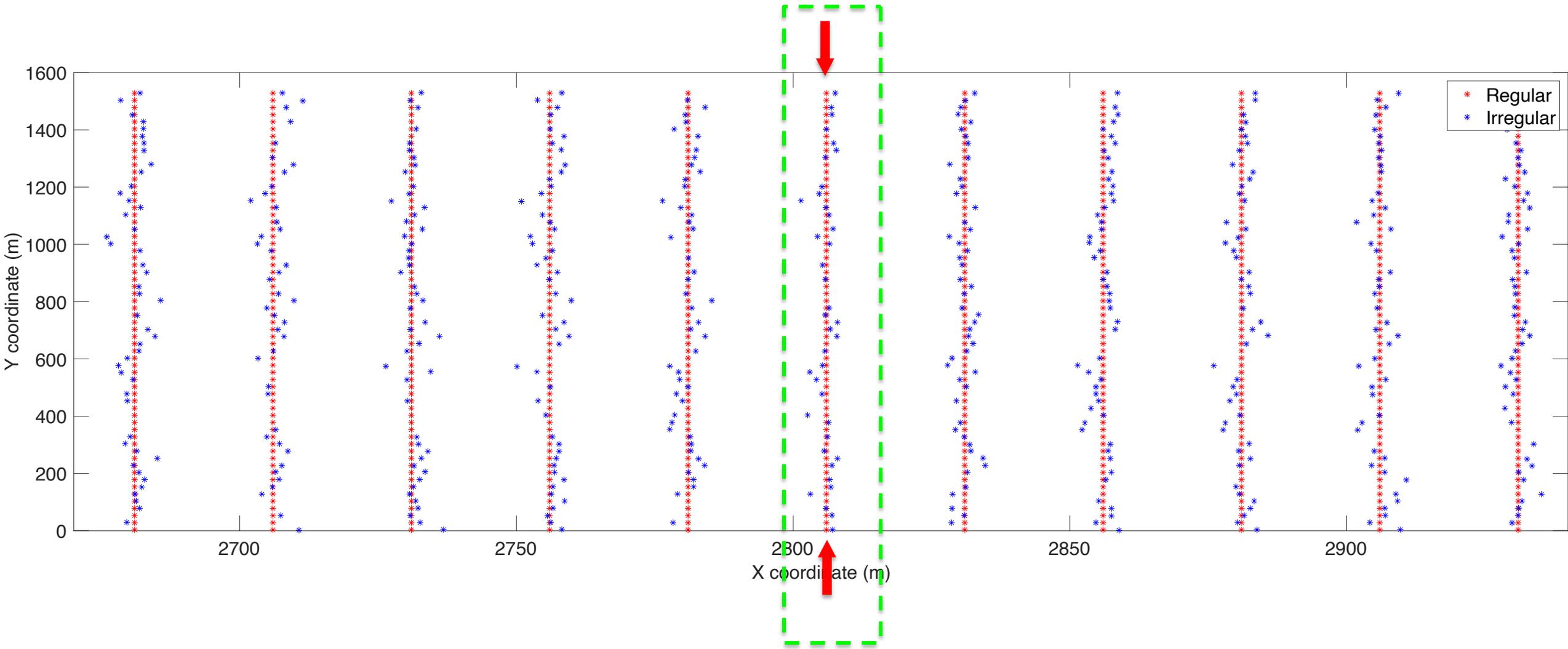
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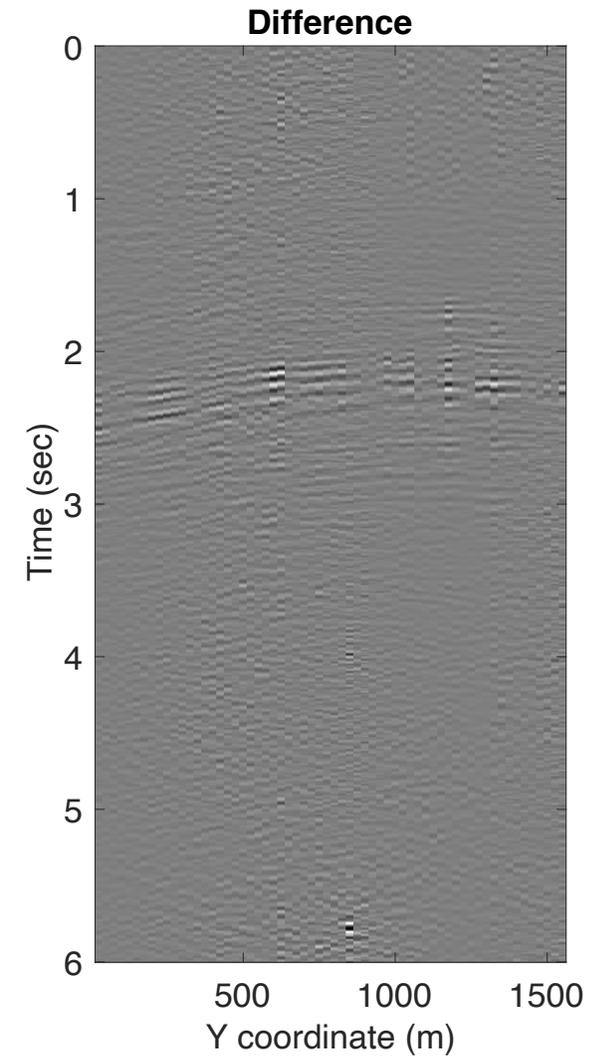
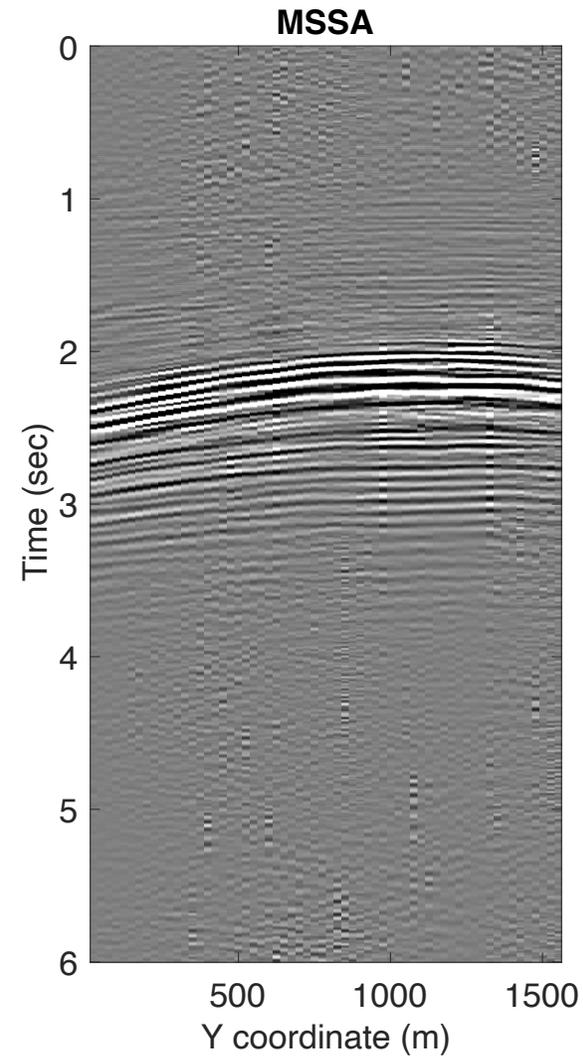
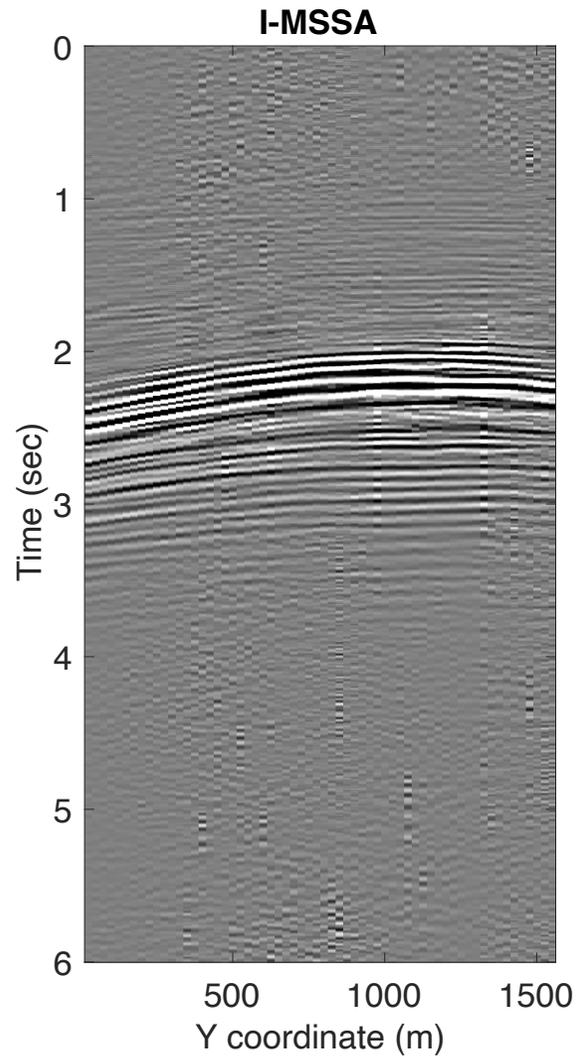
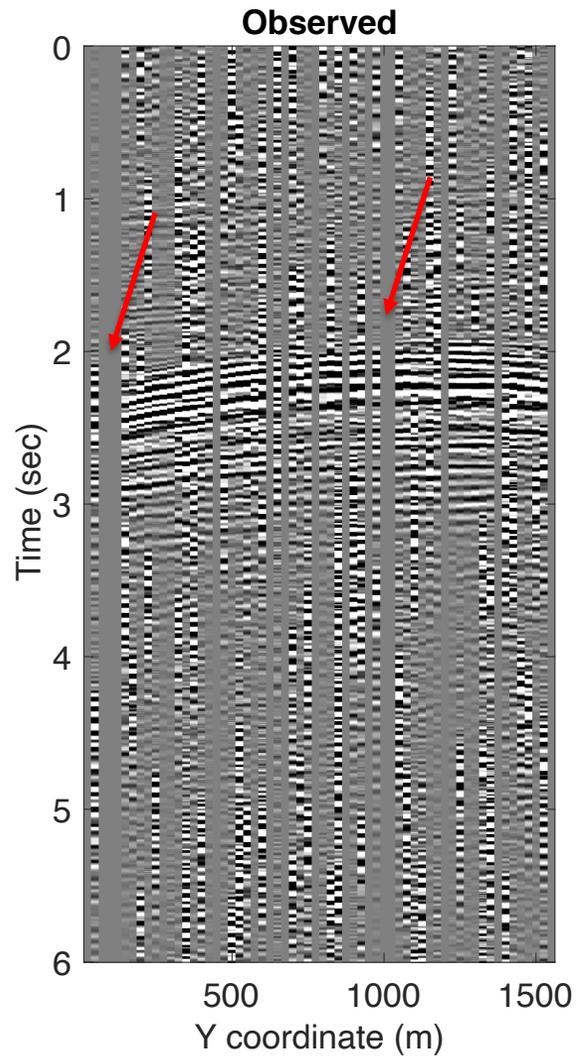
- Inline number = 51



- Crossline number = 112



- Crossline number = 112



- The I-MSSA method is a useful tool for **irregular grid seismic data reconstruction**.
- The I-MSSA in conjunction with the **Projected Gradient Descent Method** was used to deblending and shots reconstruction simultaneously.
- We do not have a **ground truth solution** for our real data test. Hence, we cannot evaluate precisely and QC the deblending and reconstruction results. However, we believe that experiments with synthetics show that it is important to avoid binning errors. Therefore, **IMSSA should be preferentially used rather than MSSA in combination of source position binning**.
- More real datasets for tests would benefit this research, so if you can provide data, it will be appreciated.

- The sponsors of the Signal Analysis and Imaging Group (SAIG) at the University of Alberta.